

Semiconductor Devices II

Part 2

Chapter 3: Contact resistance

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[Outline] Chapter 3: Contact resistance

Resistance scaling - general

- Contact resistance
- Quantum limit of resistance
- How to measure contact resistance

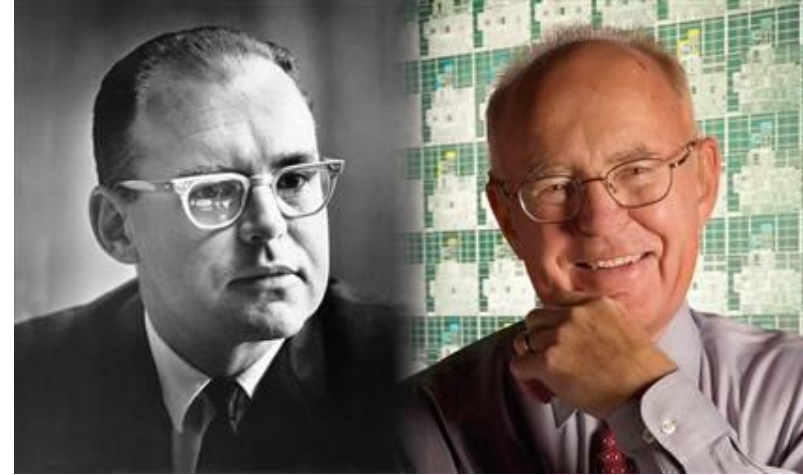
Contacts to 2D materials

- Contact geometries
- Contact resistance scaling
- Strategies for reducing the contact resistance

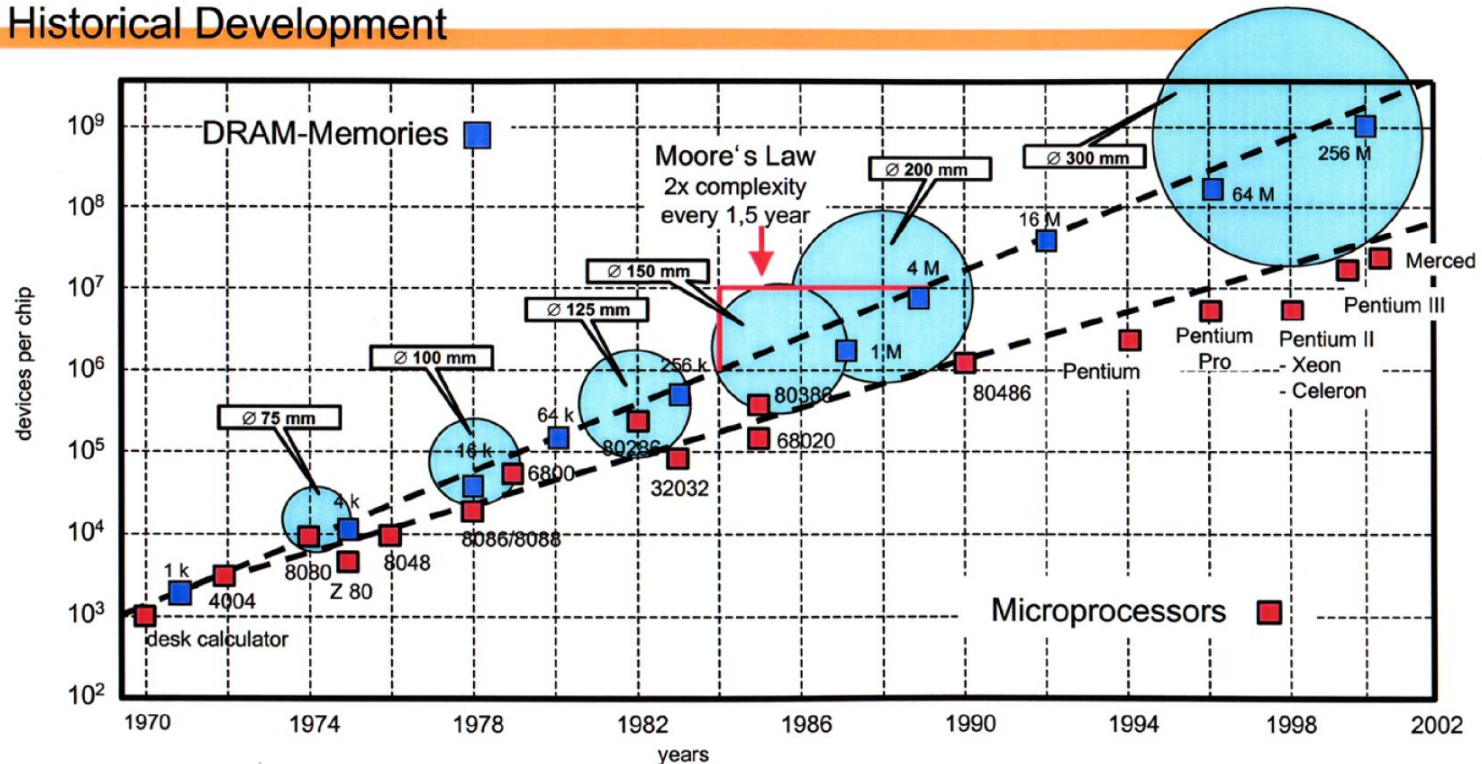
Moore's Law

Gordon Moore, co-founder of Intel stated in 1965:

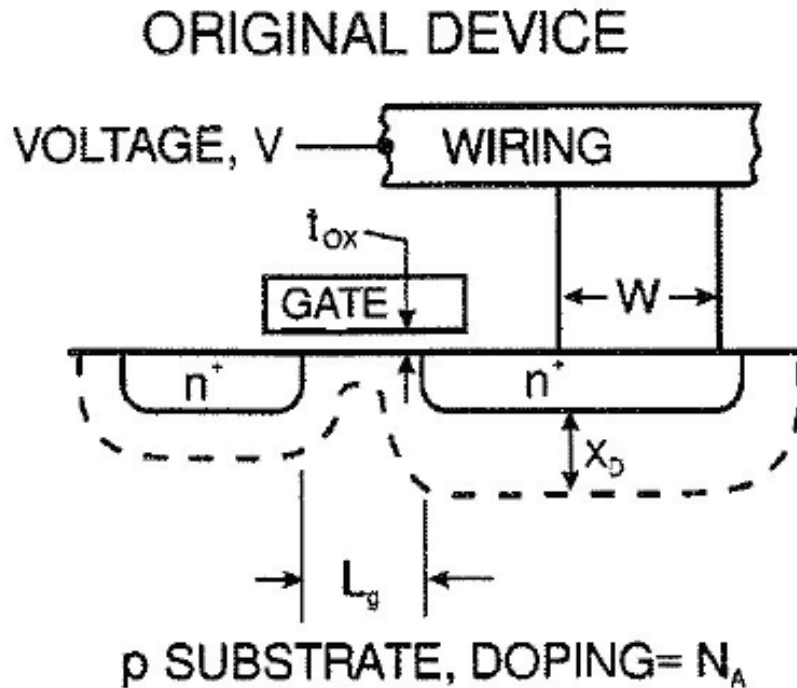
“The number of transistors that can be inexpensively placed on an integrated circuit is increasing exponentially, doubling approximately every two years”



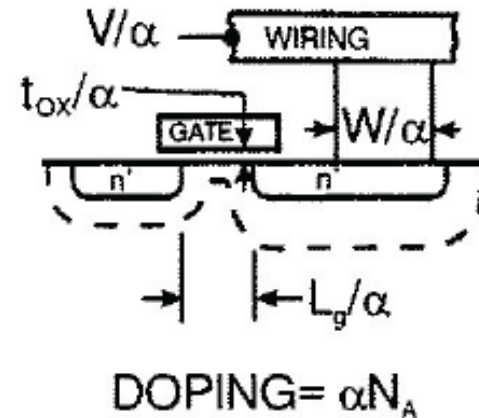
Historical Development



CMOS Scaling: Dennard Scaling (IBM)



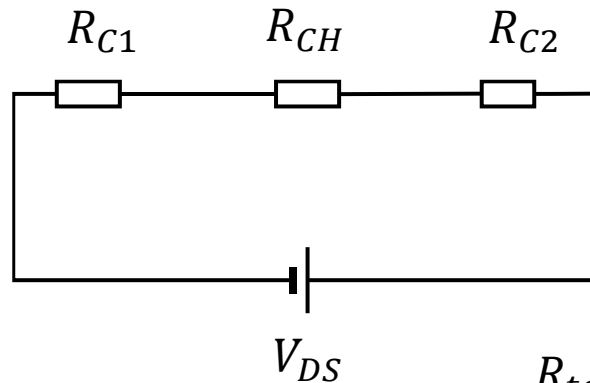
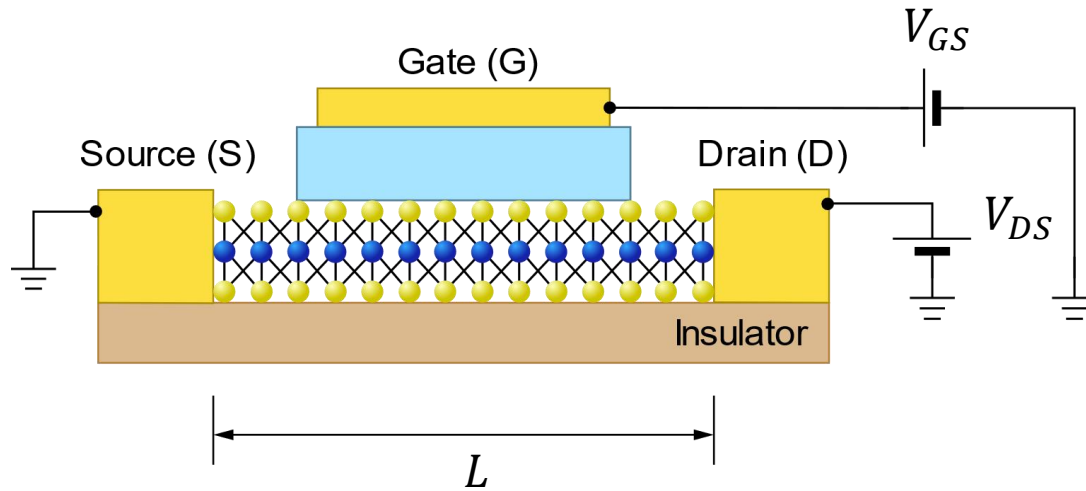
SCALED DEVICE



R. H. Dennard et al.,
IEEE J. Solid State Circuits, (1974).

If the **dimensions**, **dopant concentrations** and **voltages** are scaled as shown, according to simple electrostatics the **electric field configuration** will be exactly the same

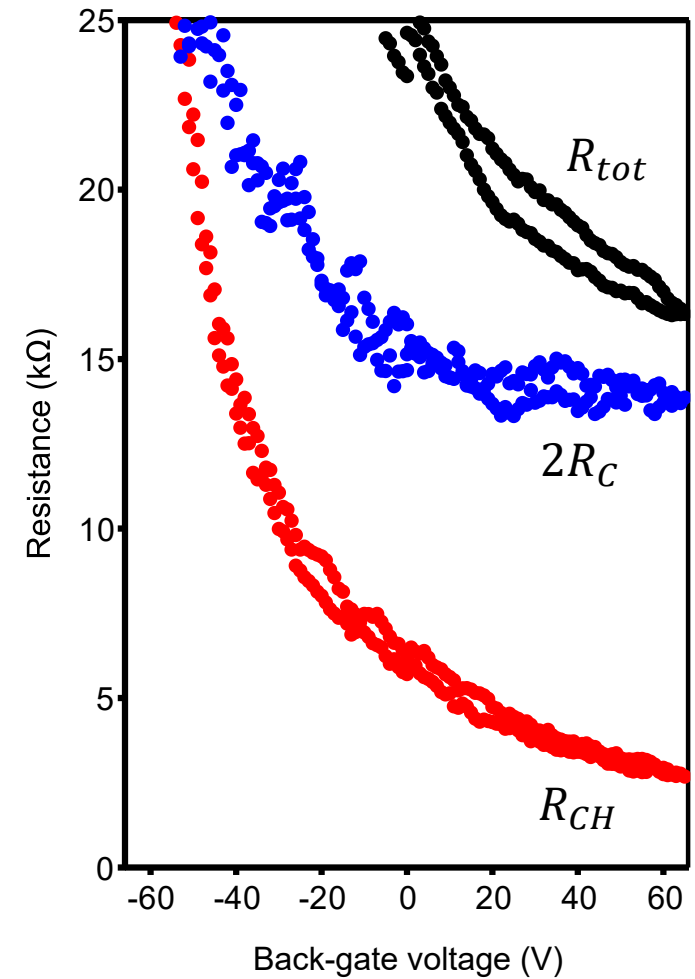
Contact resistance in practice



$$R_{tot} = R_{CH} + R_{C1} + R_{C2}$$

$$R_{tot} = R_{CH} + 2R_C$$

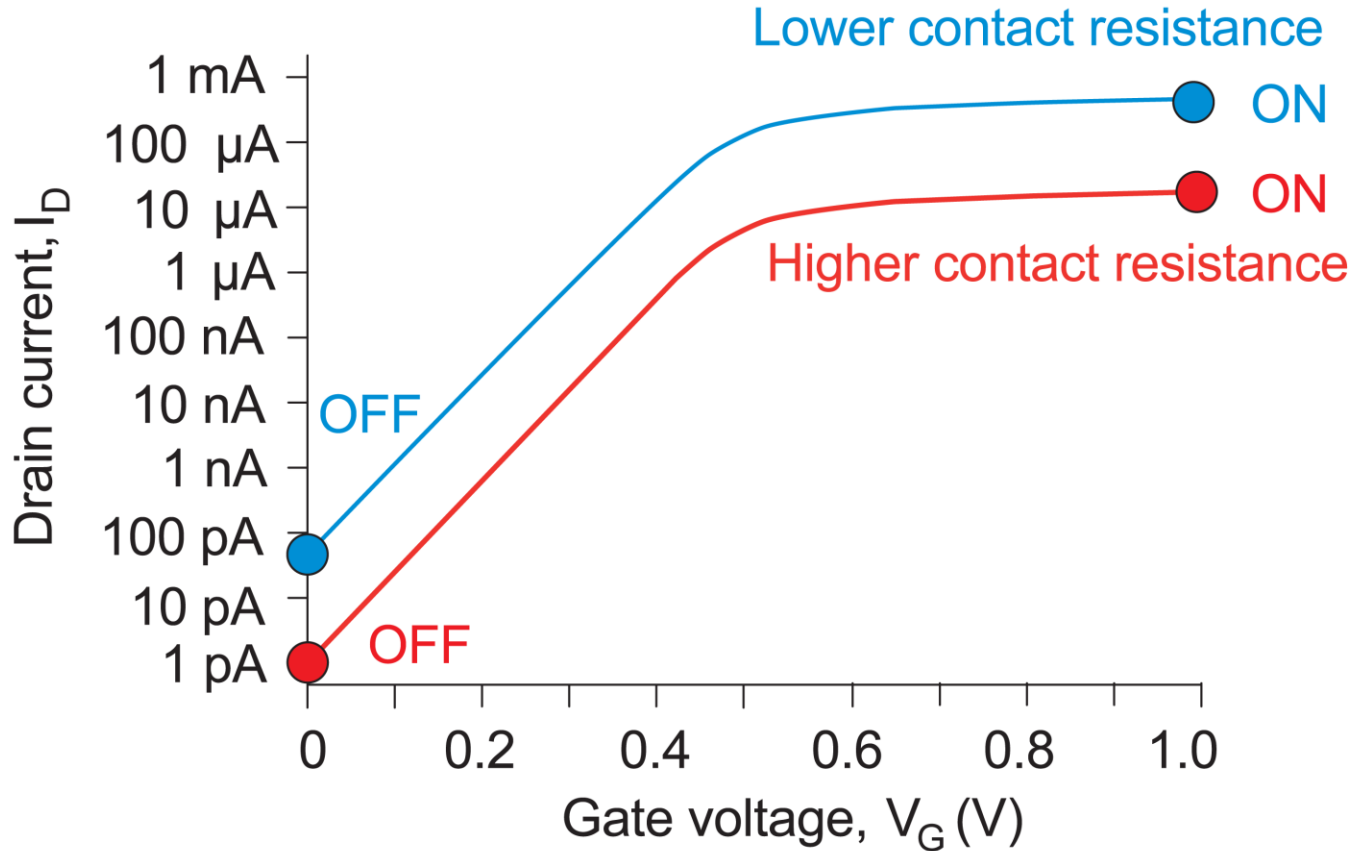
Scales with L



Allain et al., ACS Nano (2014)

R_{CH} channel resistance
 R_{C1}, R_{C2} individual contact resistances
 R_{tot} total resistance

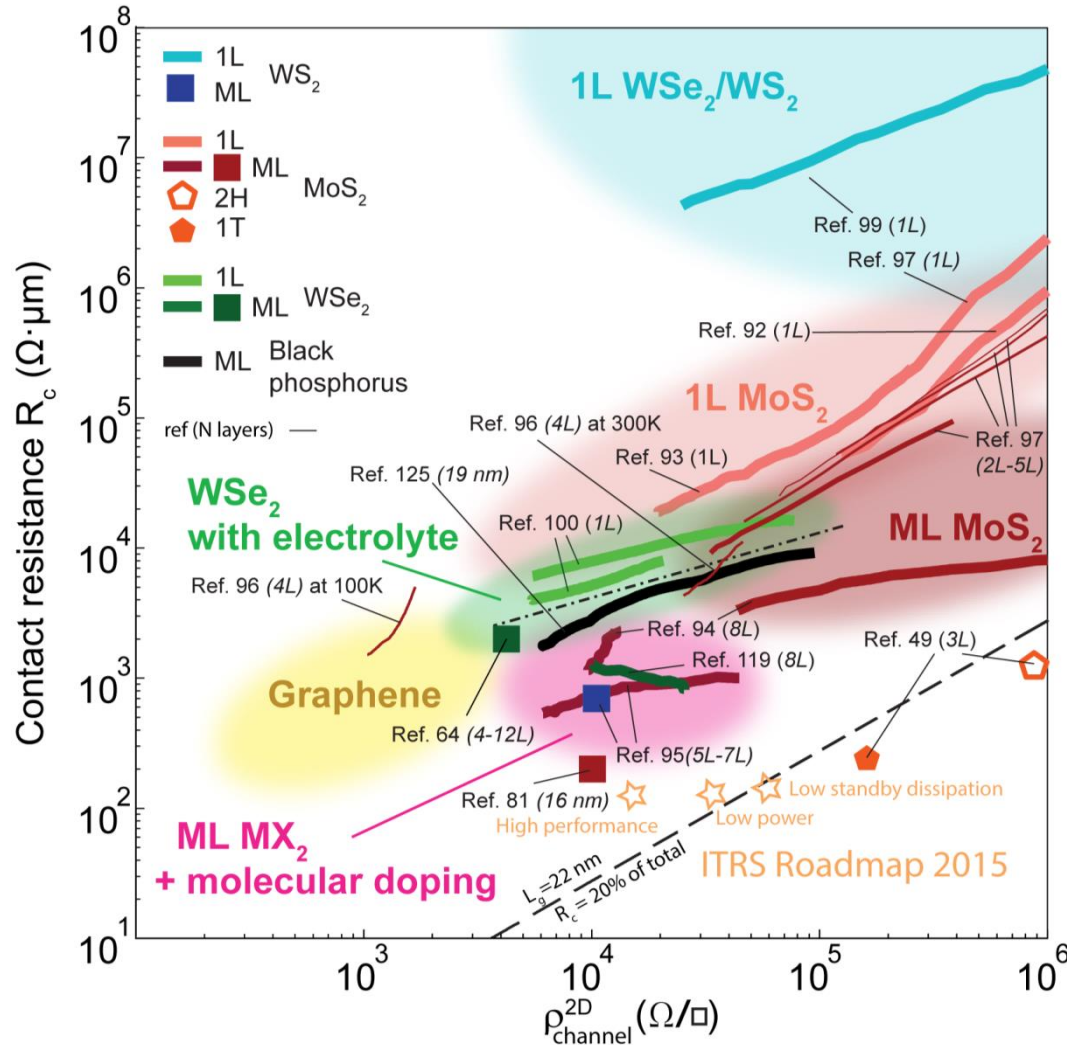
Influence on FET characteristics



How much contact resistance can we tolerate?

$$2R_C < 20\% \text{ of } R_{tot}$$

ITRS 2012 requirement for low-standby-power SOI FETs



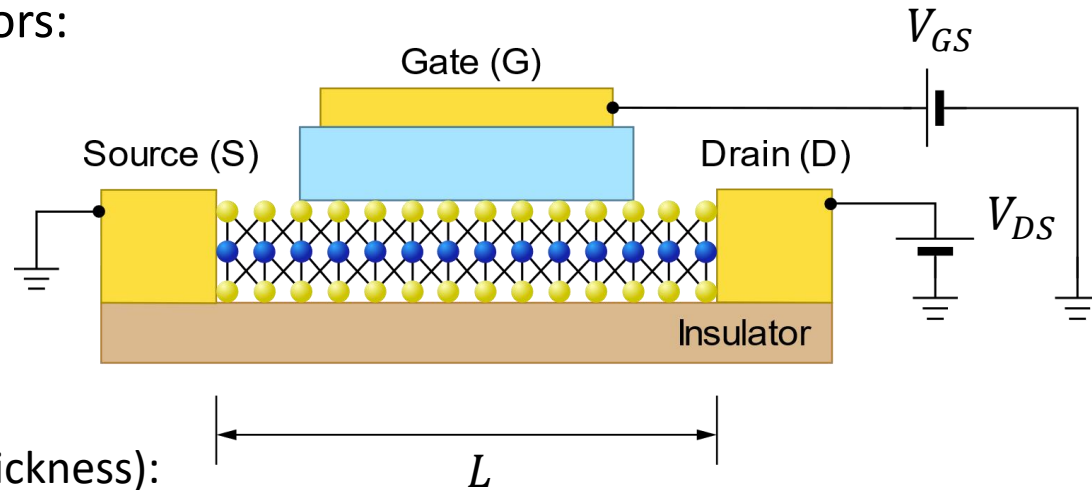
Allain...Bannerjee, Kis; Nature Materials (2015)

How far can we go: quantum limit of resistance

For macroscopic ($L \gg l_m$) conductors:

Ohm's law $I_{DS} = \frac{V_{DS}}{R}$

Resistance $R = \rho \frac{L}{S}$



Resistance for a 2D material (no thickness):

$$R = \rho_{2D} \frac{L}{W}$$

Resistance scaling $L \rightarrow 0$ ($L < l_m$):

$$\lim_{L \rightarrow 0} R = 0 \quad \text{Mathematics}$$

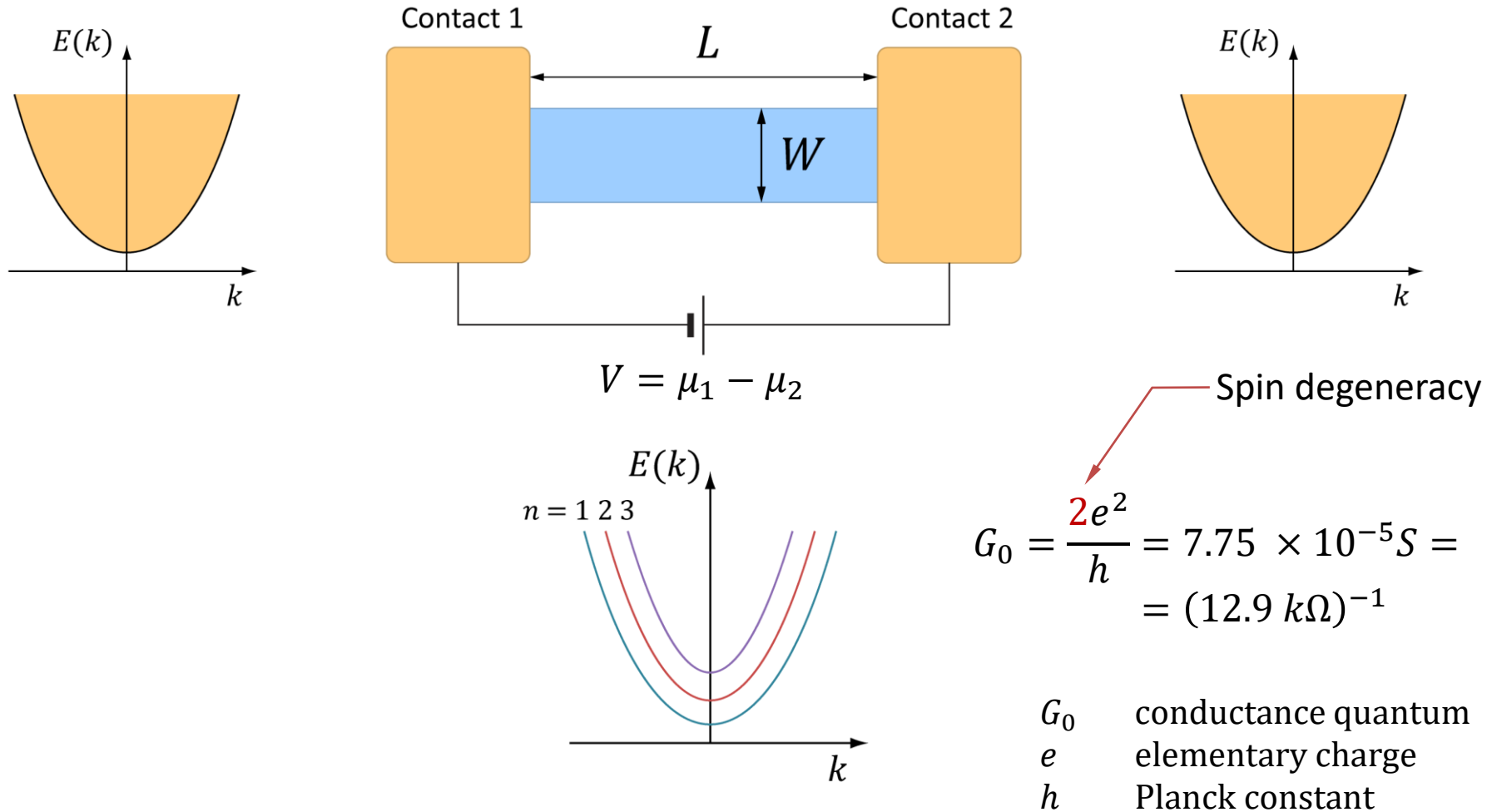
$$\lim_{L \rightarrow 0} R = R_C \quad \text{Reality}$$

l_m	elastic mean free path (1-10 nm for 2D semiconductors)
ρ	resistivity
ρ_{2D}	2D resistivity
L	length
S	cross-sectional area
W	width
R_C	contact resistance (on the order of k Ω)

There is a fundamental, quantum limit on how far the resistance can scale!

Quantum resistance

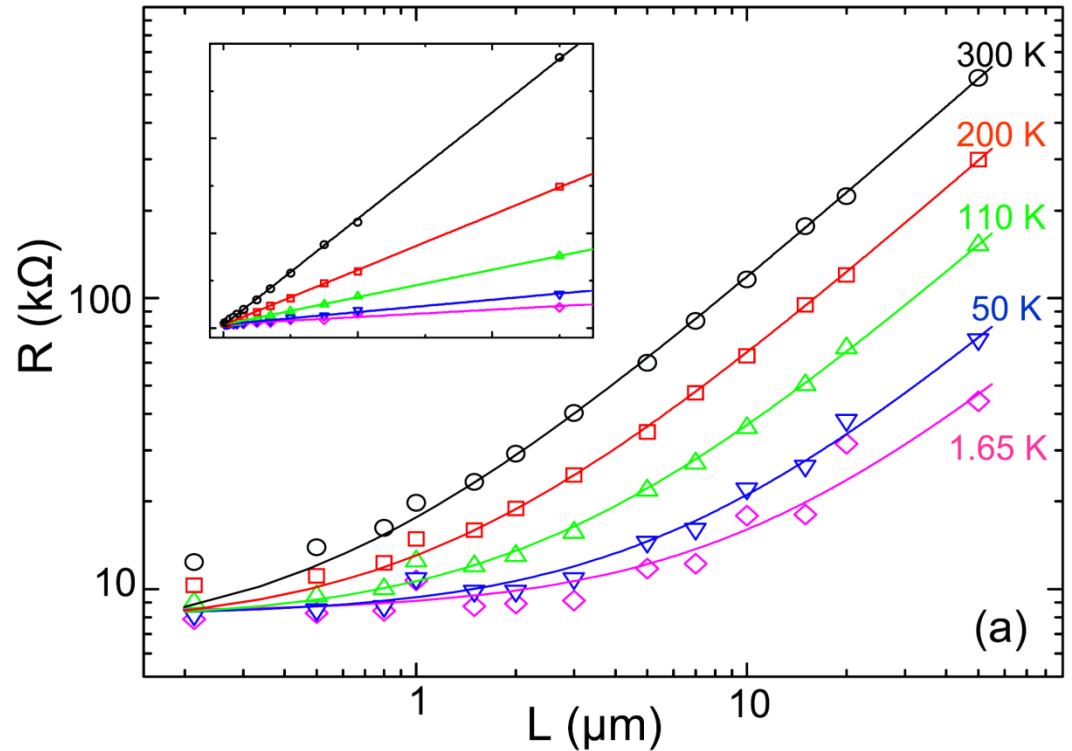
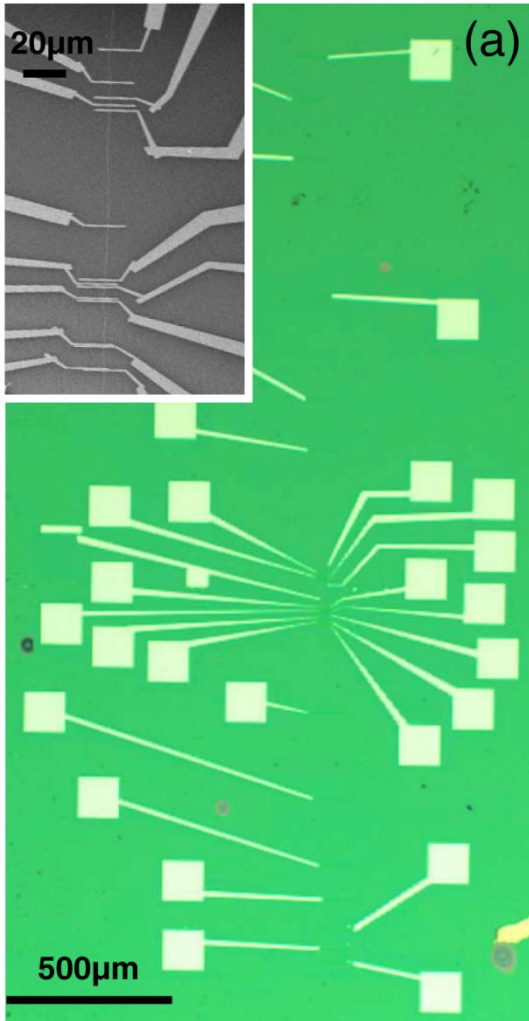
As the dimensions decrease, resistance approaches a limiting value R_C



Origin: conductor and contact pads are dissimilar materials (with and without quantum confinement)

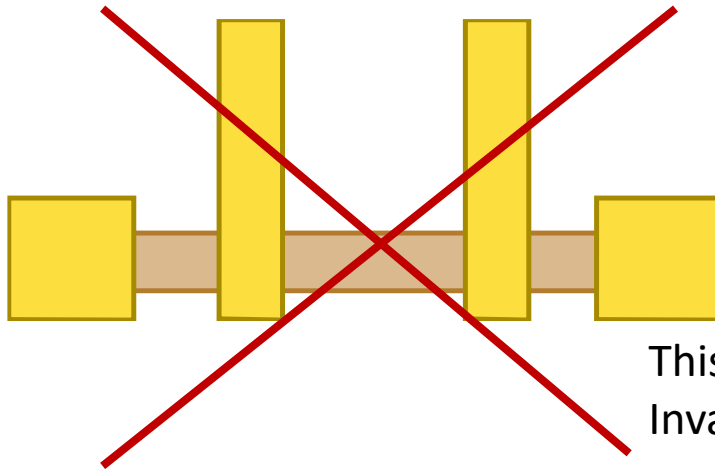
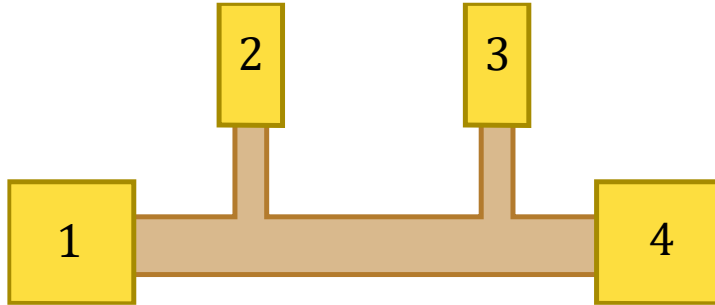
Example: carbon nanotube

Several millimeters long carbon nanotube, with multiple contacts

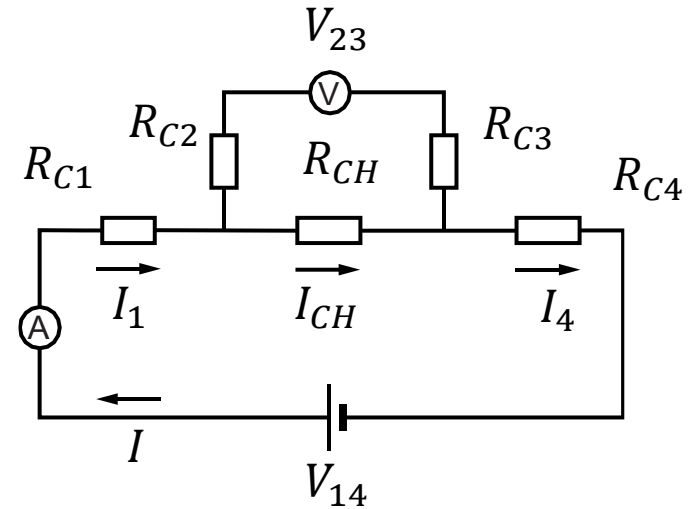


Purewal et al., PRL 98, 186808 (2007)

Contact resistance measurements - 4 probe technique



This is not a 4C device!
Invasive contacts!



$$R_{CH} = \frac{V_{23}}{I} \quad R_{tot} = \frac{V_{14}}{I}$$

$$2R_C = \frac{V_{14} - V_{23}}{I}$$

Internal resistance of the voltmeter must be high so there is no current flowing through it:

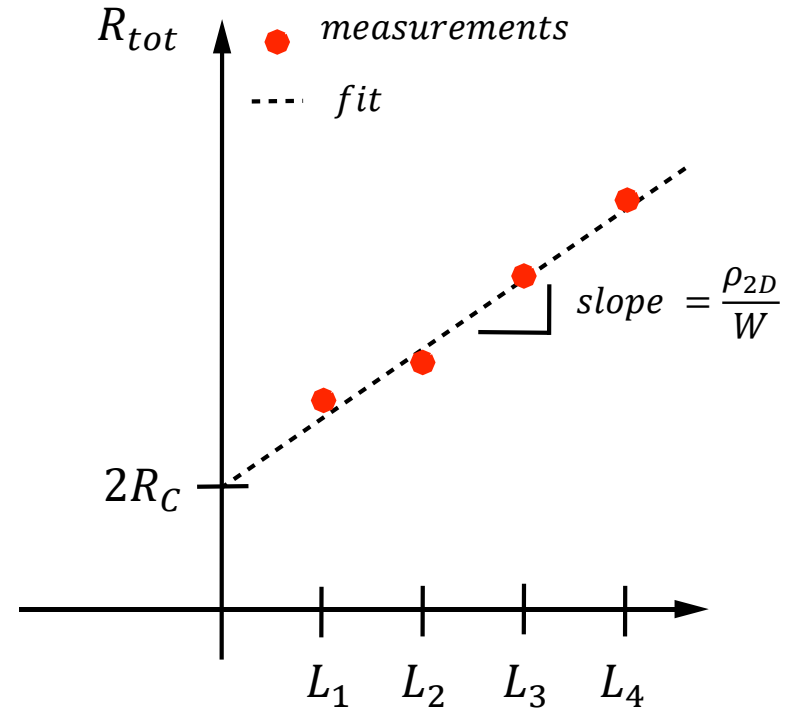
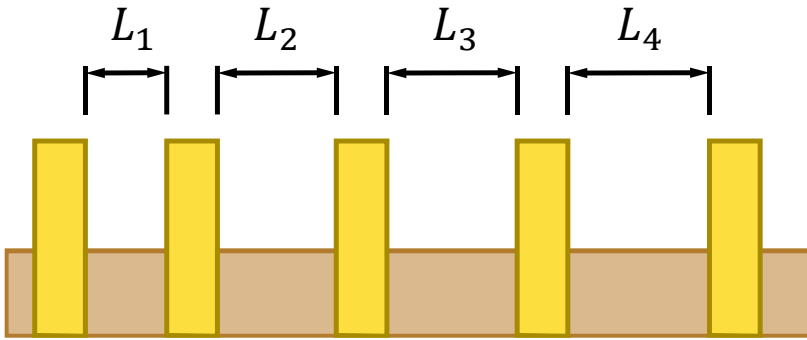
$$I_1 = I_{CH} = I_4 = I$$

Contact resistance measurements – TLM

Transmission line measurements;
transfer length method

Resistance for a 2D material w contacts:

$$R_{tot} = \rho_{2D} \frac{L}{W} + 2R_C$$

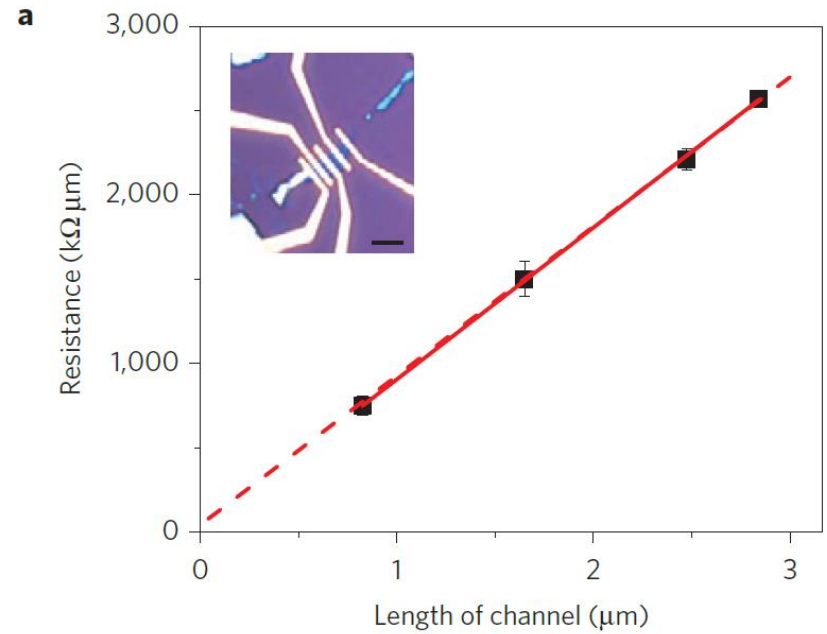
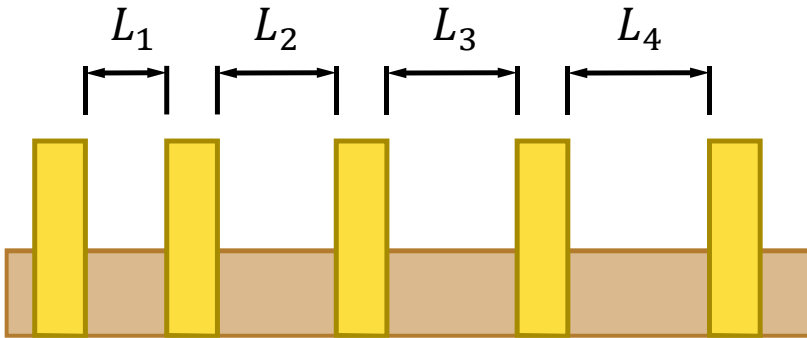


Contact resistance measurements – TLM

Transmission line measurements;
transfer length method

Resistance for a 2D material w contacts:

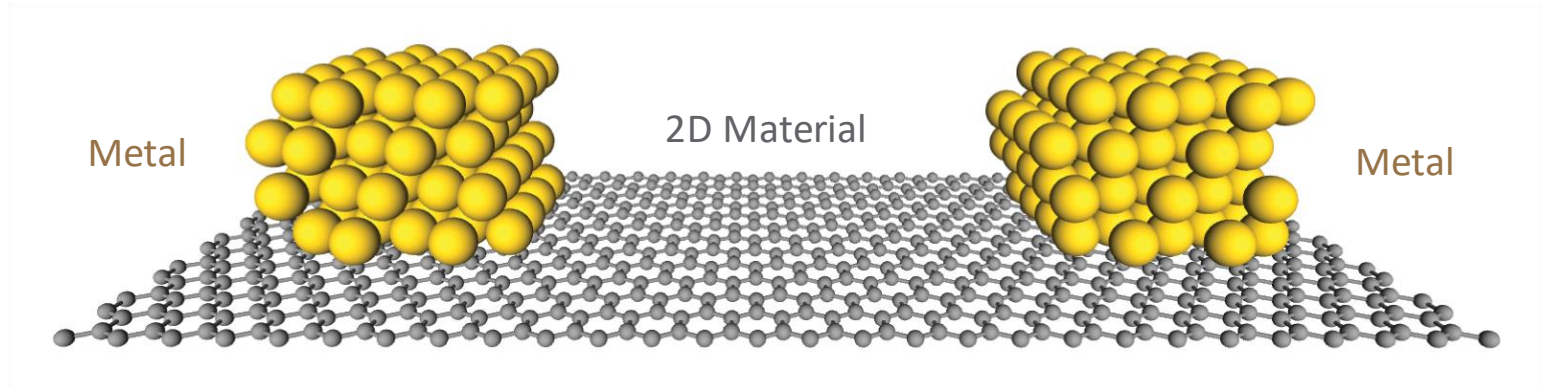
$$R_{tot} = \rho_{2D} \frac{L}{W} + 2R_C$$



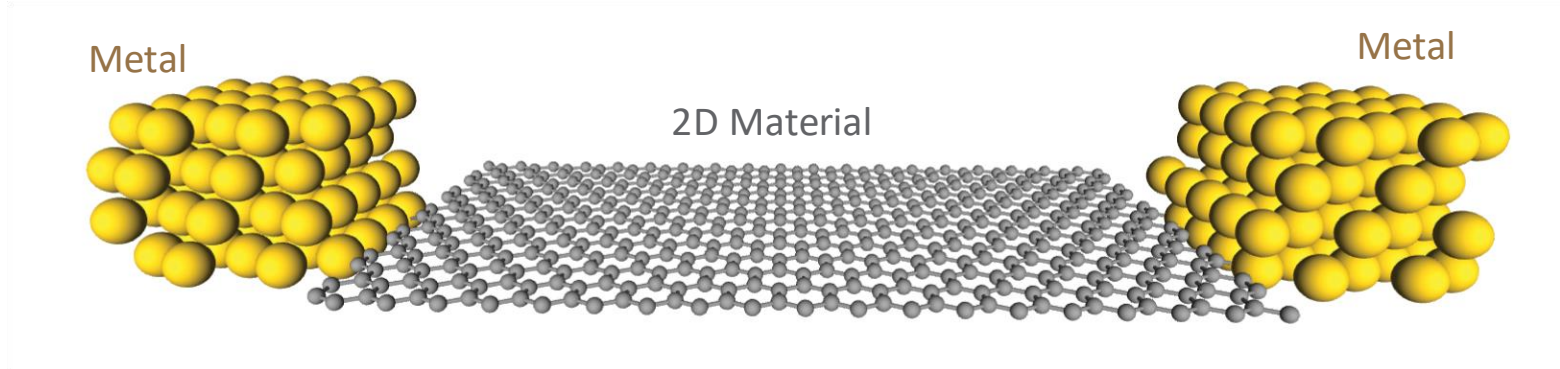
Koppera et al., Nature Materials (2014)

Contact geometry

Top-Contact

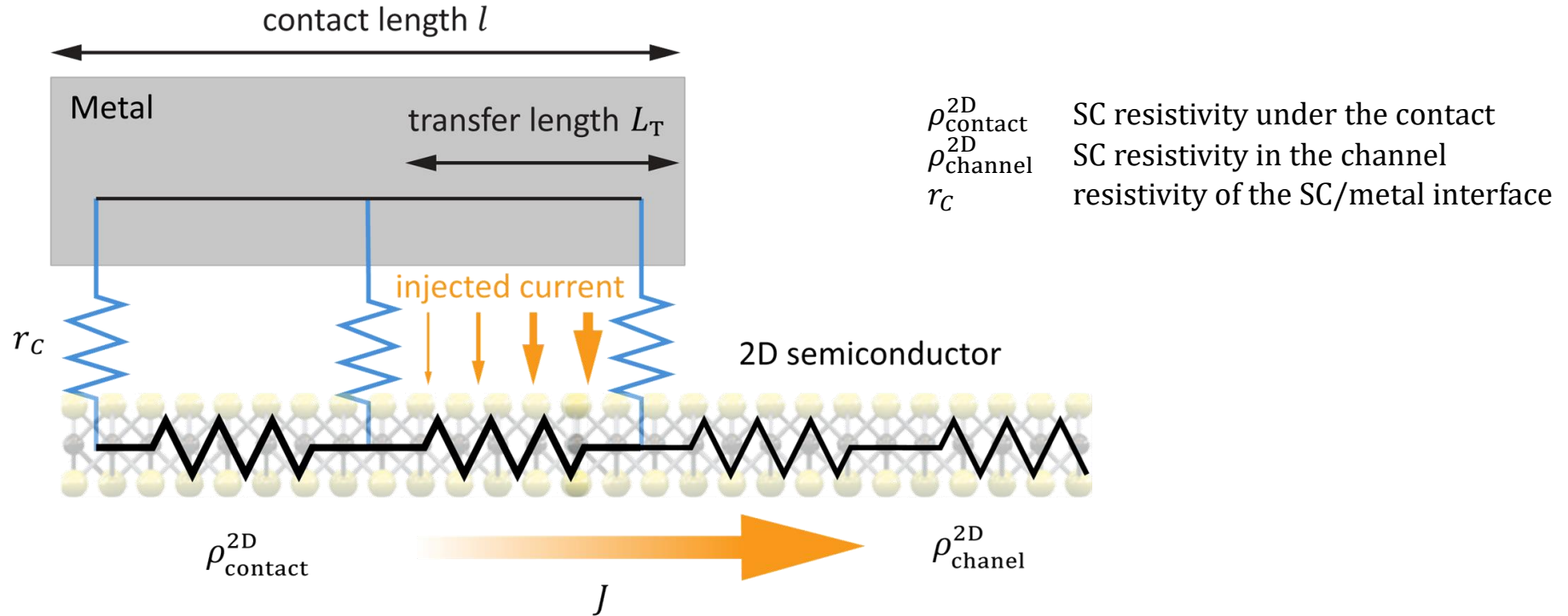


Edge-Contact



Contact resistance scaling

Transmission line model, current crowding:



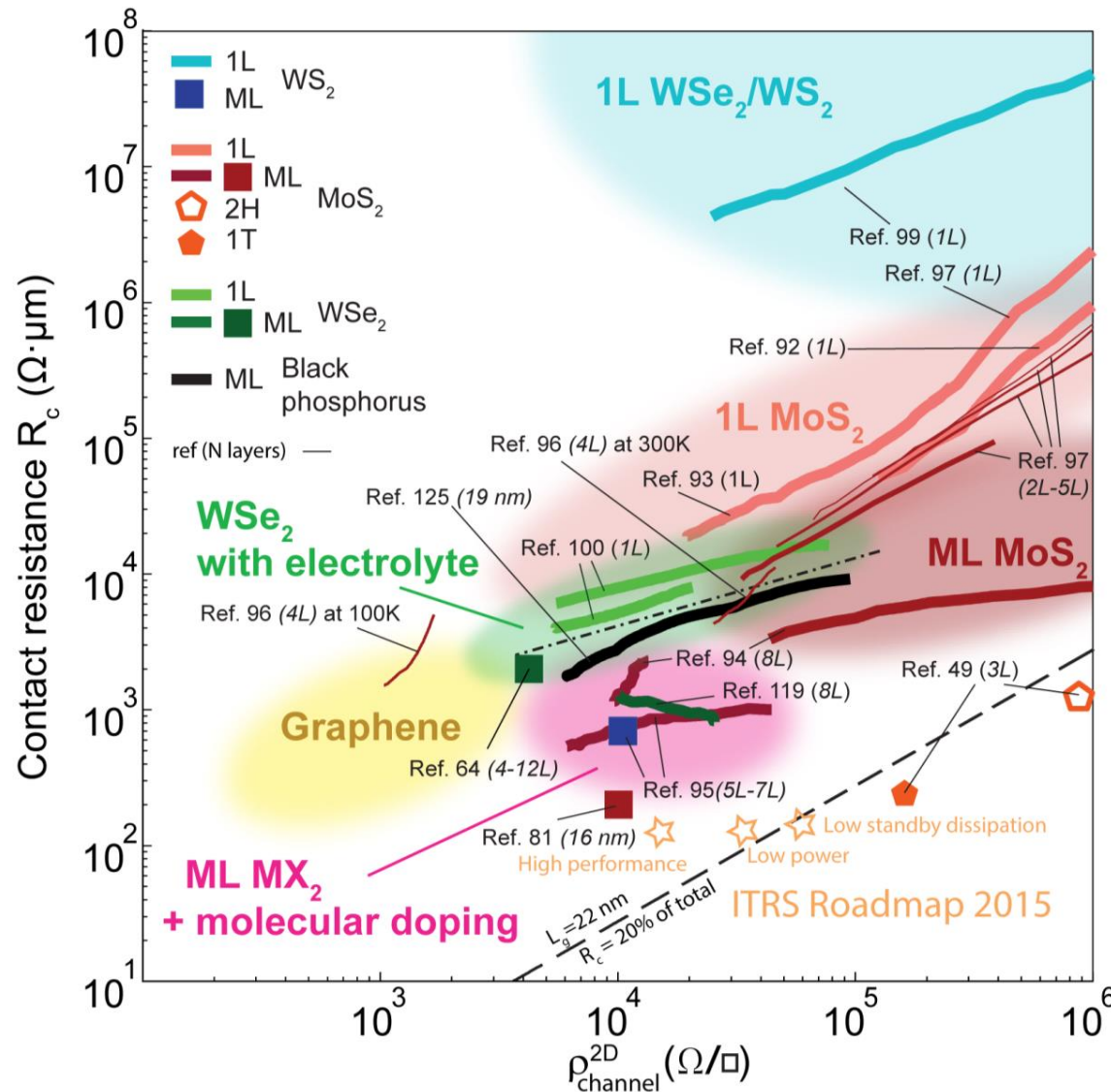
Common assumption: $\rho_{\text{contact}}^{2D} = \rho_{\text{channel}}^{2D}$

$$R_C = \sqrt{\rho^{2D} r_c} \coth \left(l \sqrt{\rho^{2D} / r_c} \right) \quad \text{for } l \gg L_T = \sqrt{r_c / \rho^{2D}} : \quad R_C = \sqrt{\rho^{2D} r_c}$$

$$L_T = 20 - 600 \text{ nm}$$

Independent of l !

Experimental review



State of the art

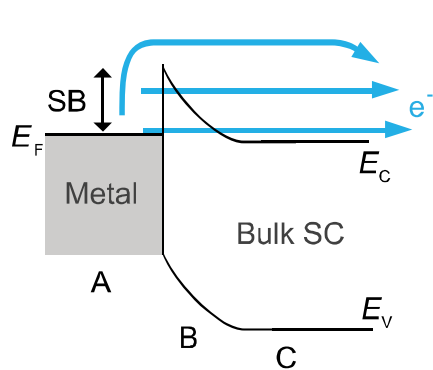
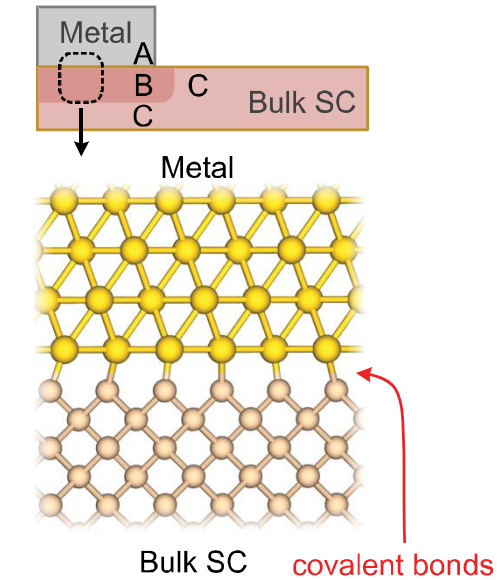
$$R_c = 200 - 300 \Omega \cdot \mu\text{m}$$

Theoretical limit

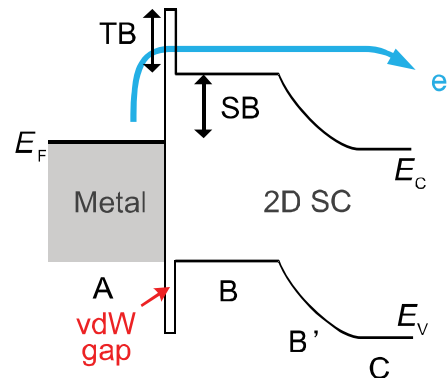
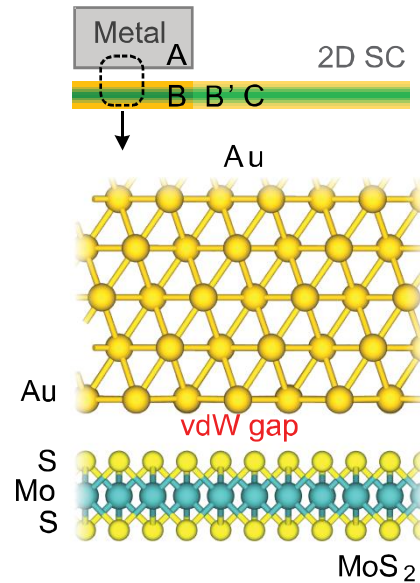
$$R_c = 30 \Omega \cdot \mu\text{m} \text{ for } n_{2D} = 10^{13} \text{ cm}^{-2}$$

Electrical contacts to 2D materials

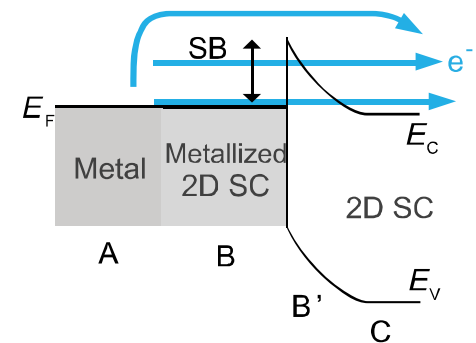
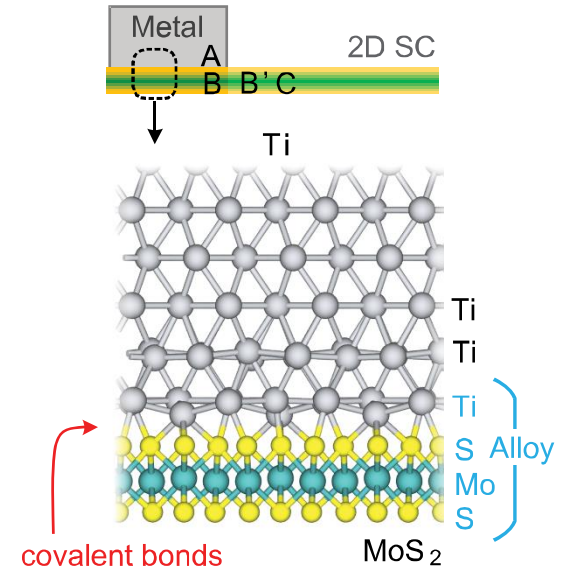
Metal – Bulk SC Contact



Metal - 2D SC Contact
(with vdW Gap)



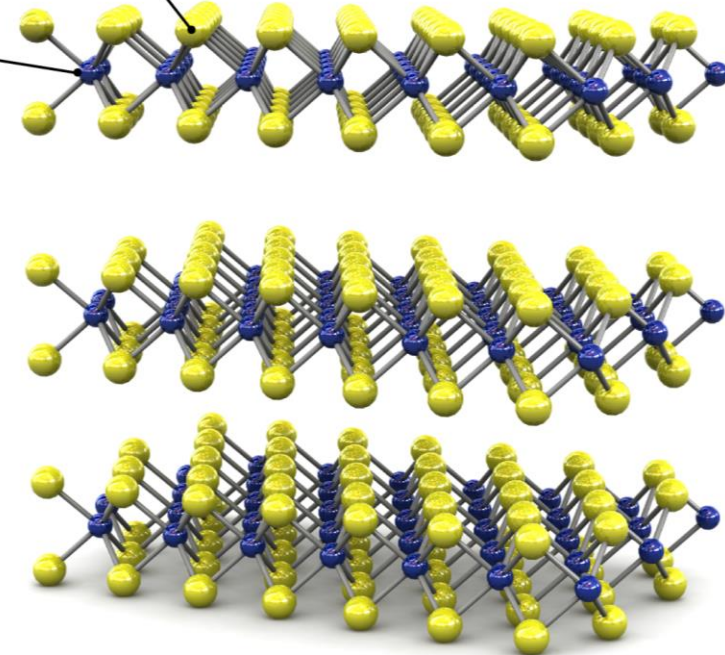
Metal - 2D SC Contact
(with Hybridization)



2D Transition Metal Dichalcogenides (TMDCs)

H																		He
Li	Be											B	C	N	O	F	Ne	
Na	Mg											Al	Si	P	S	Cl	Ar	
K	Ca	Sc	Ti	V	Cr	Mn	Fe	Co	Ni	Cu	Zn	Ga	Ge	As	Se	Br	Kr	
Rb	Sr	Y	Zr	Nb	Mo	Tc	Ru	Rh	Pd	Ag	Cd	In	Sn	Sb	Te	I	Xe	
Cs	Ba	Ln	Hf	Ta	W	Re	Os	Ir	Pt	Au	Hg	Tl	Pb	Bi	Po	At	Rn	
Fr	Ra	An	Rf	Db	Sg	Bh	Hs	Mt	Ds	Rg								
			La	Ce	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Ho	Er	Tm	Yb	Lu	
			Ac	Th	Pa	U	Np	Pu	Am	Cm	Bk	Cf	Es	Fm	Md	No	Lr	

- Common formula: MX_2
- 40 stable materials



Semiconductors: MoS_2 $MoSe_2$ WS_2 WSe_2
 $MoTe_2$ WTe_2

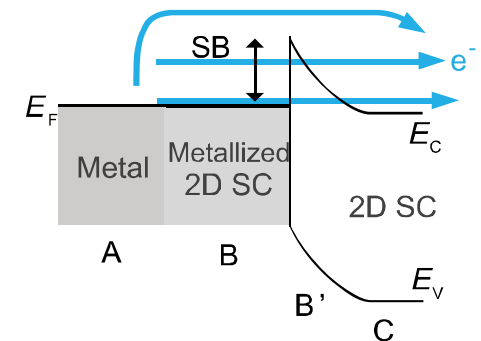
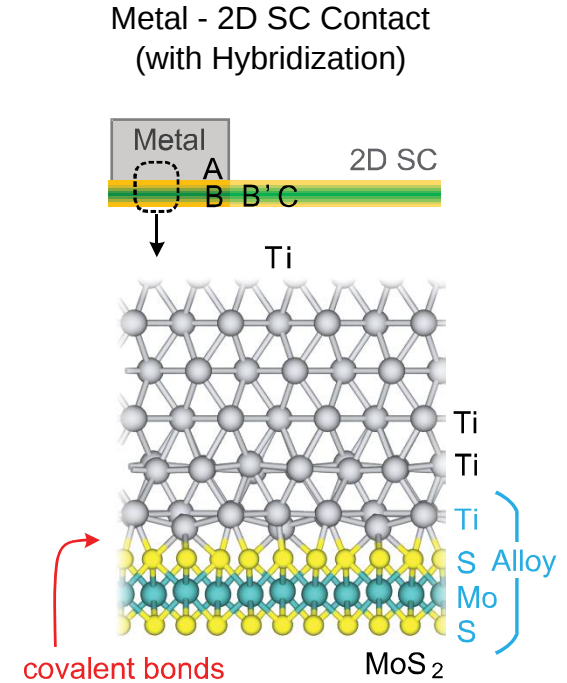
Semimetals: TiS_2 $TiSe_2$

Metals, CDW,
 superconductors: $NbSe_2$ NbS_2 $NbTe_2$
 TaS_2 $TaSe_2$ $TaTe_2$

Charge-injection mechanisms

Two mechanisms:

- Thermionic emission **over** the Schottky barrier
- Field emission (tunneling) **through** the Schottky barrier



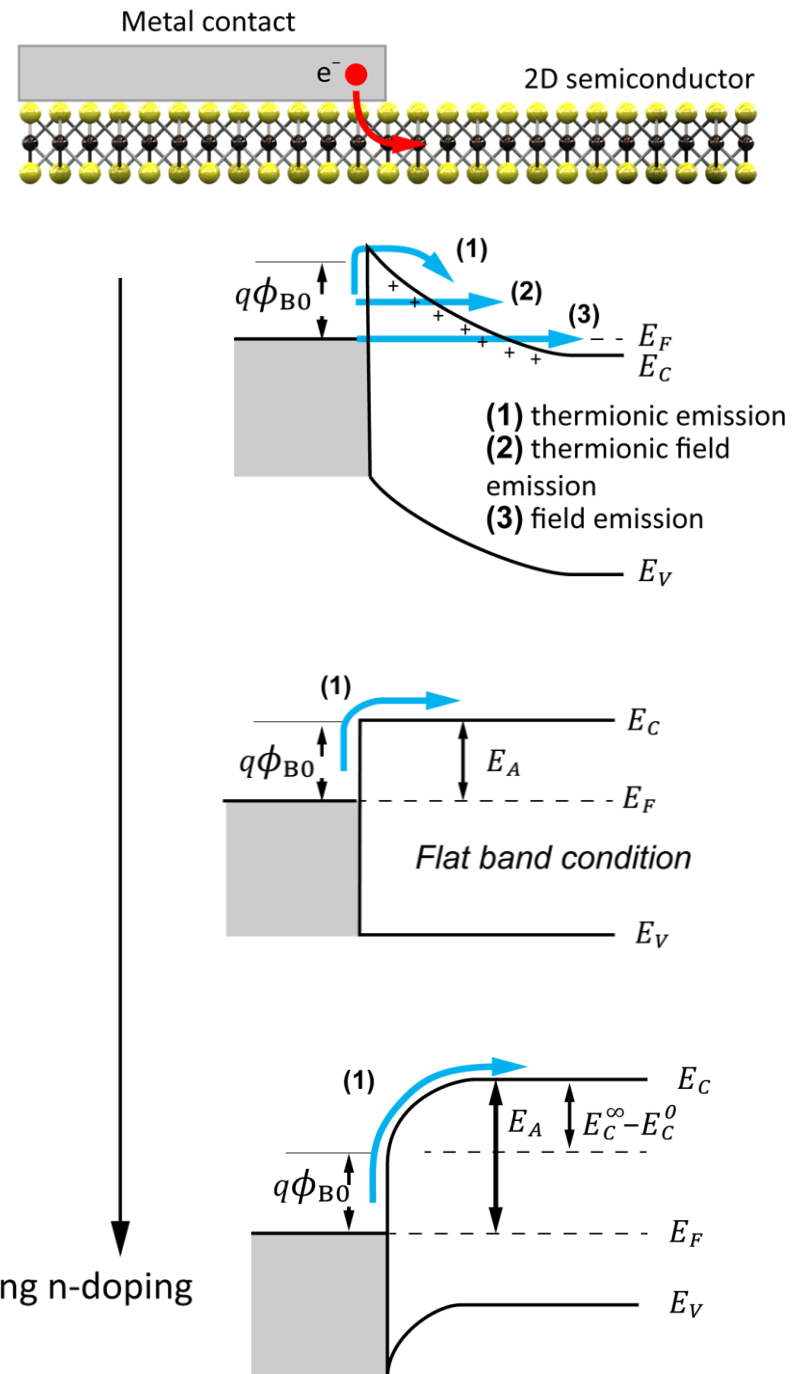
Charge-injection mechanisms

Two mechanisms:

- Thermionic emission over the Schottky barrier
- Field emission (tunneling) over the Schottky barrier

Simpler extraction of the Schottky barrier height $q\phi_{B0}$

decreasing n-doping
or V_G



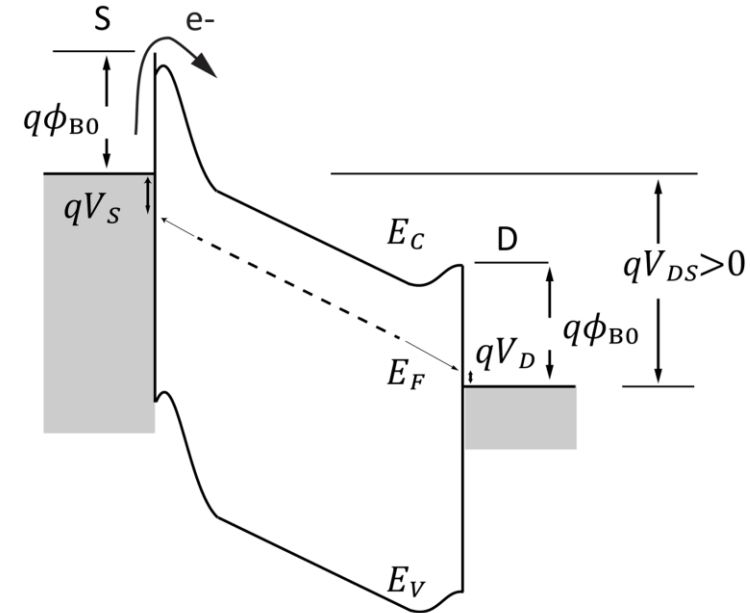
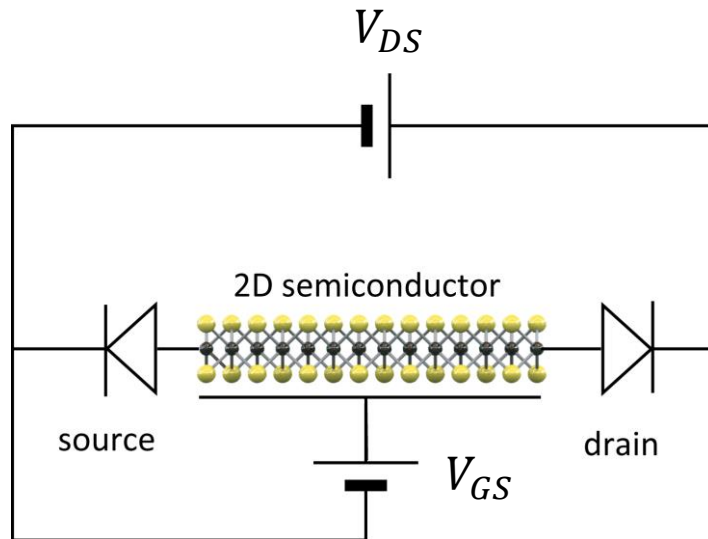
Schottky barrier height extraction

Procedure follows these points:

1. Identify contact with dominant barrier
2. Measure current, extract barrier height
3. Modify barrier height with gate voltage, extract Schottky barrier

One barrier each at source and drain:

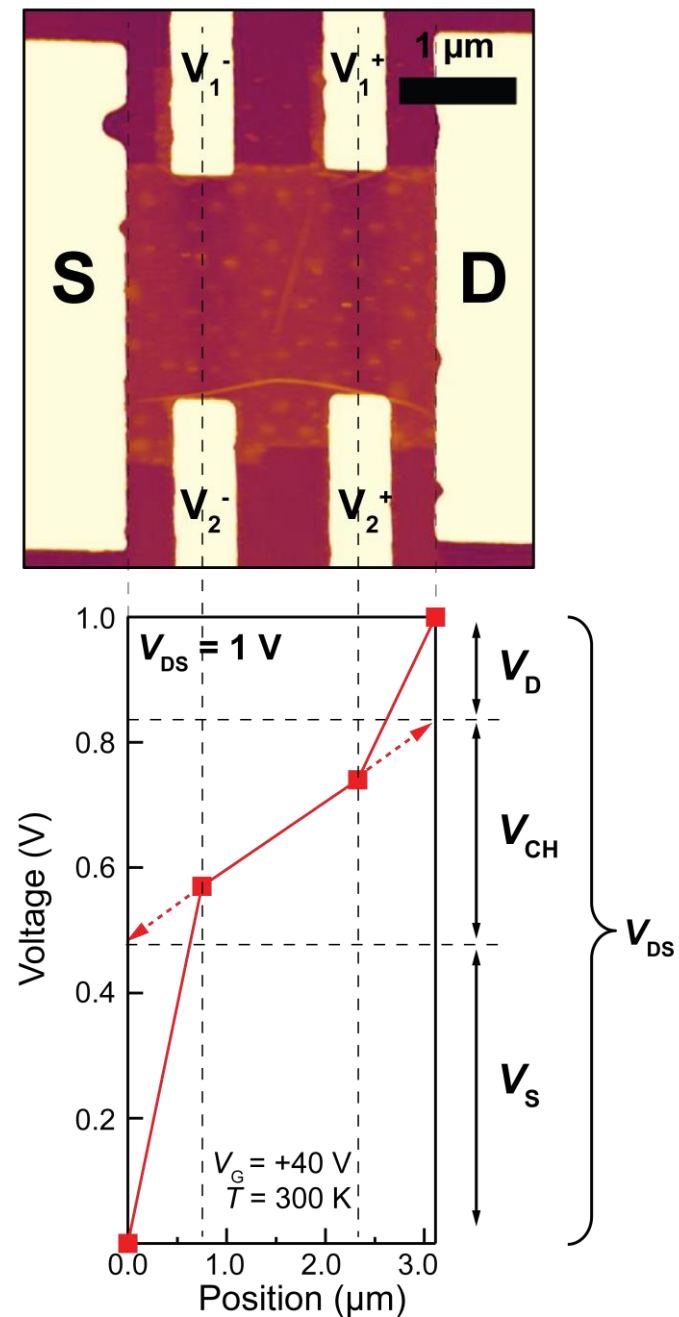
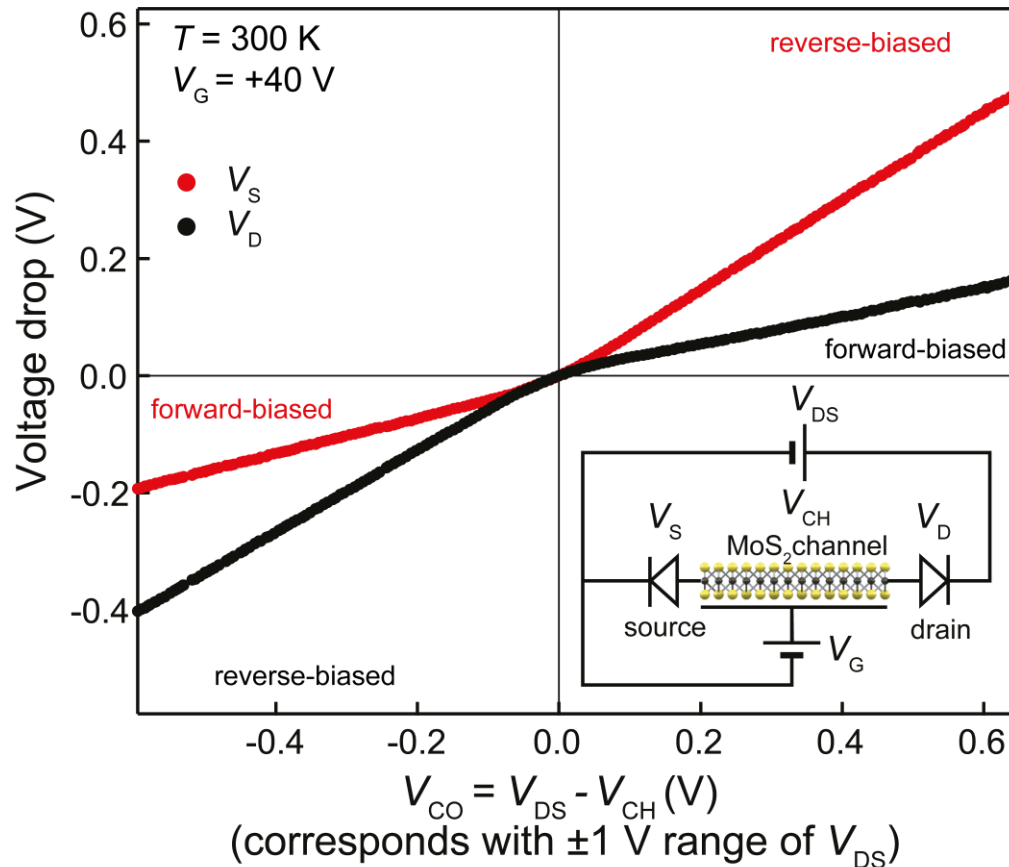
- Back-to-back connected diodes
- Biasing curve can be linear



Schottky barrier height extraction

One barrier each at source and drain:

- Back-to-back connected diodes
- Biasing curve can be linear
- Most of the voltage drop occurs on the negatively biased diode (**Point 1**)

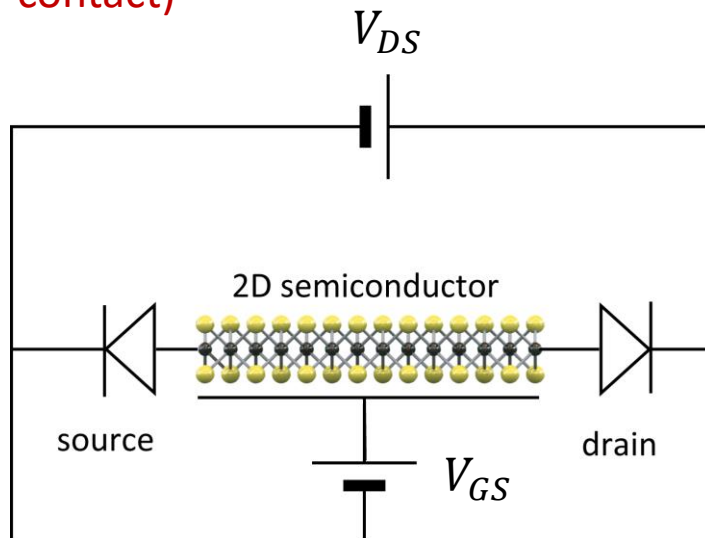


Point 1: Schottky barrier height extraction

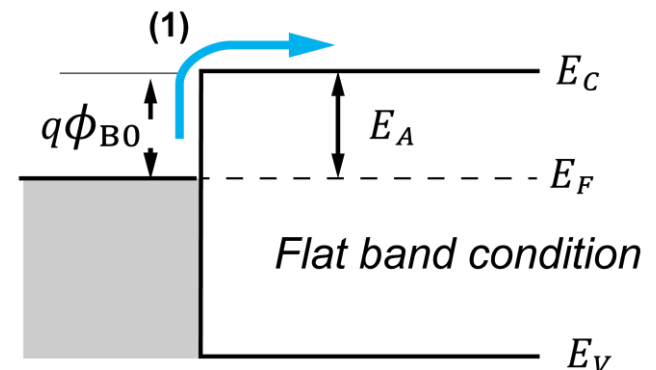
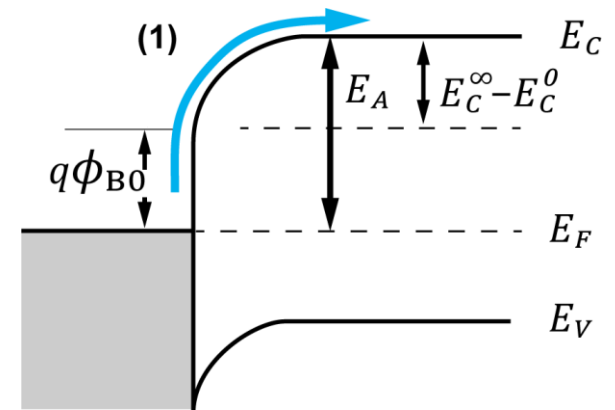
From the activation energy E_A in the thermionic emission regime

One barrier each at source and drain:

- Back-to-back connected diodes
- Biasing curve can be linear
- most of the drop occurs at the reverse-biased diode (source for n-type FET) (**Point 1: identify dominant contact**)



$$E_A = q\phi_{B0} + E_C^\infty - E_C^0$$



Point 2: Schottky barrier height extraction

Point 2: Assuming that most of the drop occurs at the reverse-biased diode (source for n-type FET), the injected current density is:

$$J = A^* T^\alpha \exp \left[-\frac{q\phi_{B0}}{k_B T} \right] \left[1 - \exp \left(-\frac{qV_{DS}}{k_B T} \right) \right]$$

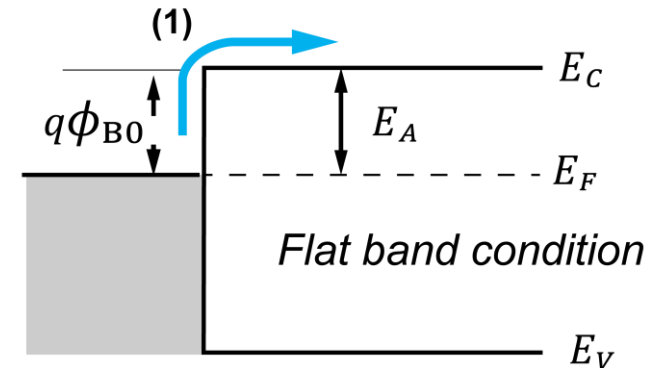
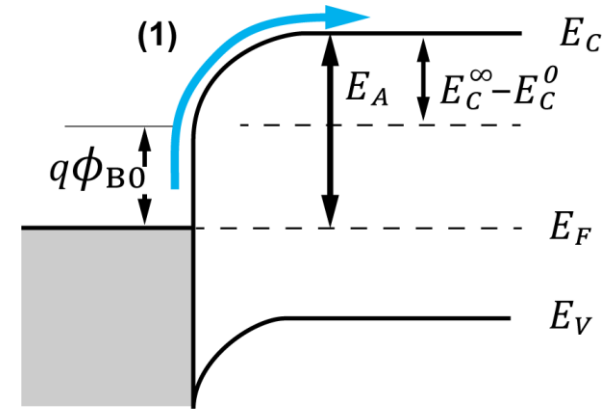
For $qV \gg k_B T$ ($k_B T \approx 20$ mV; OK until ~ 1000 K):

$$J = A^* T^\alpha \exp \left[-\frac{q\phi_{B0}}{k_B T} \right]$$

In the sub-threshold regime (low V_G):

$$J = A^* T^\alpha \exp \left[-\frac{E_A}{k_B T} \right] \quad E_A = q\phi_{B0} + \underbrace{E_C^\infty - E_C^0}$$

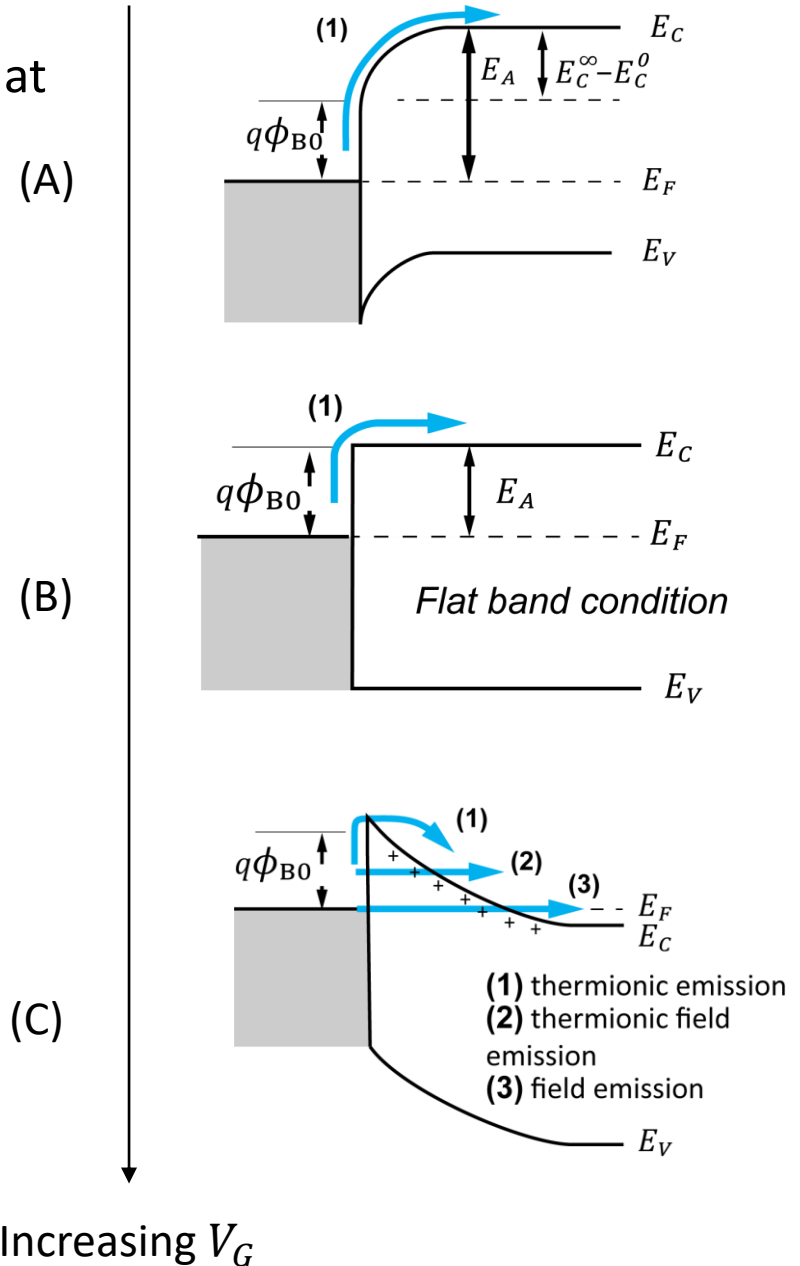
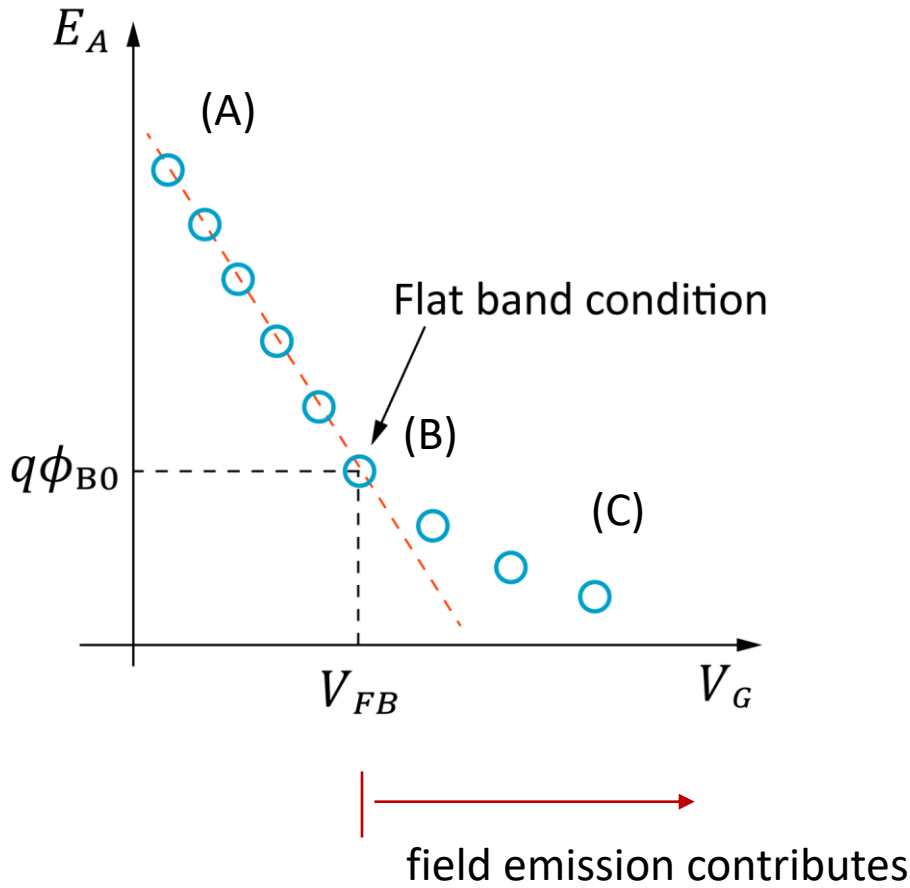
Difference between the conduction bands in the bulk (∞ , far from the contact) and at the interface (0)



A^* Richardson constant
 ϕ_{B0} Schottky barrier height
 α 2 for bulk SC, 3/2 for 2D

Point 3: Schottky barrier height extraction

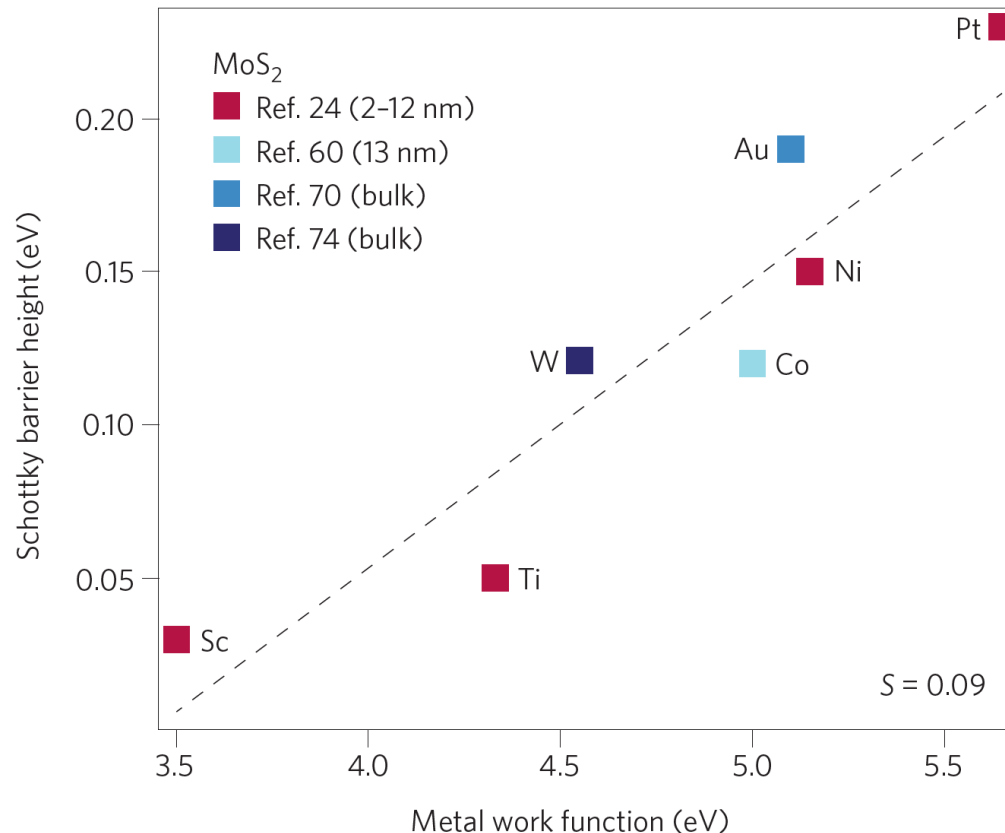
Point 3: Extract E_A as a function of V_G , identify flat band voltage V_{FB} :



Schottky barrier height

Fermi level pinning

- Metal – 2D SC alloy
- Gap states because of weaker S - Mo bonding
- Choice of metals for contacts alone not the most suitable strategy for reducing R_C



Allain...Bannerjee, Kis; Nature Materials (2015)

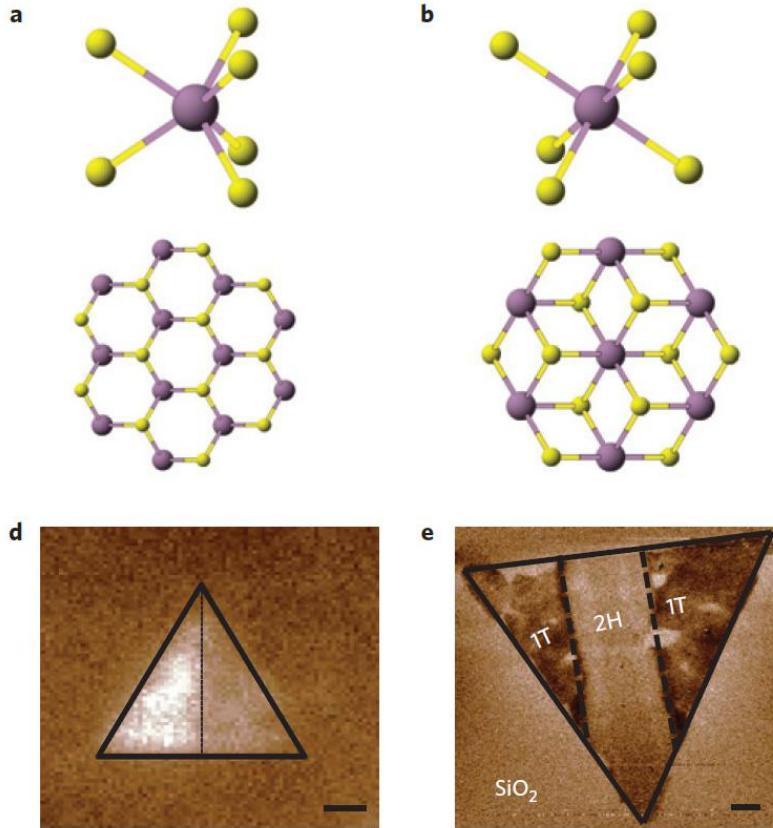
Strategies for reducing contact resistance

Several strategies appear promising:

- Phase engineering
- Doping
- Edge contacts
- Direct transfer

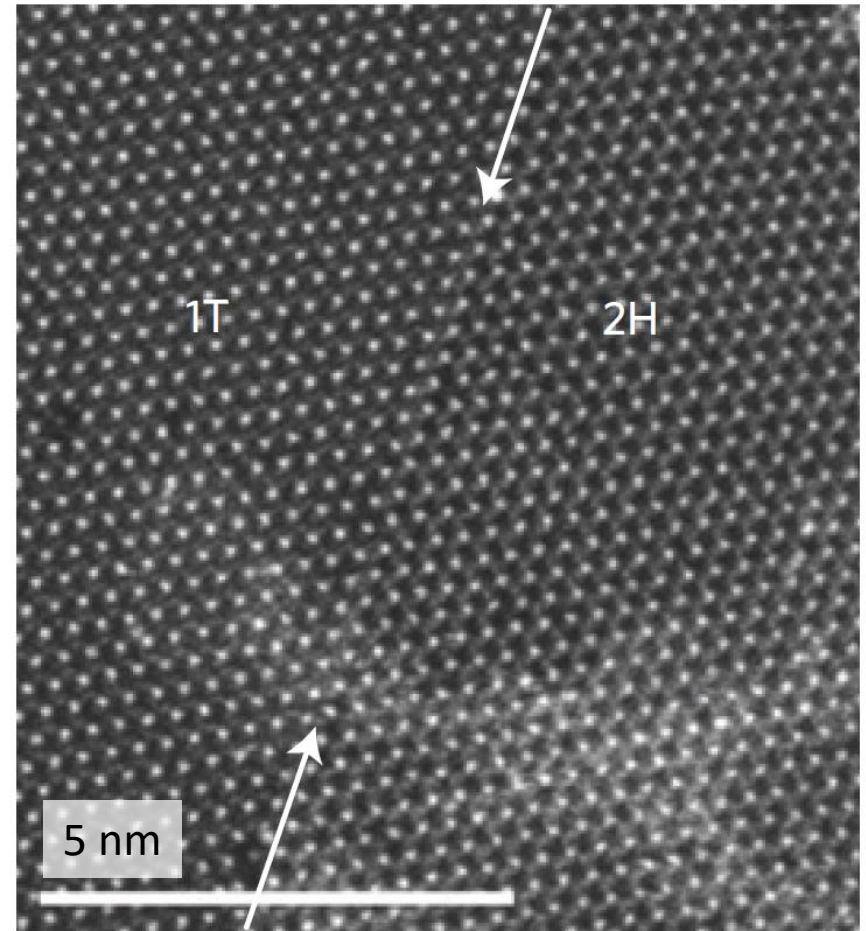
Phase engineering

Heavy doping by Lithium can trigger a phase transition into a metallic phase



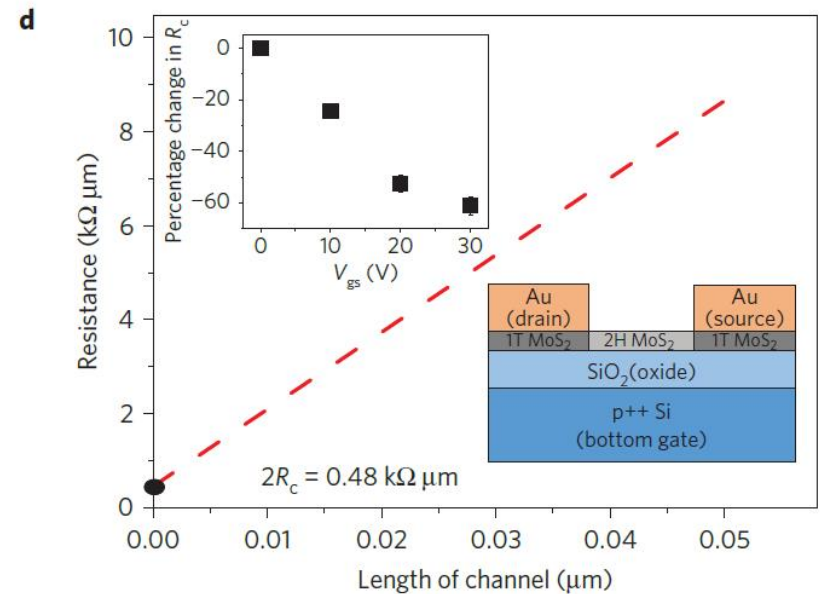
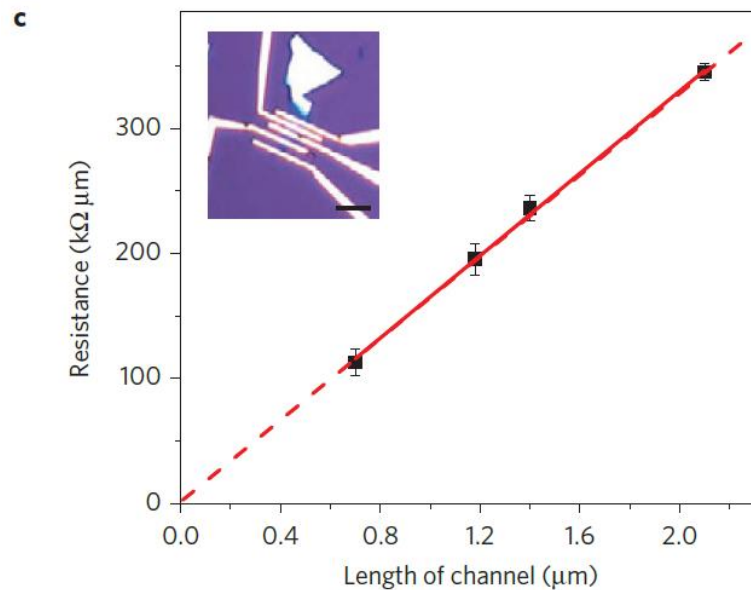
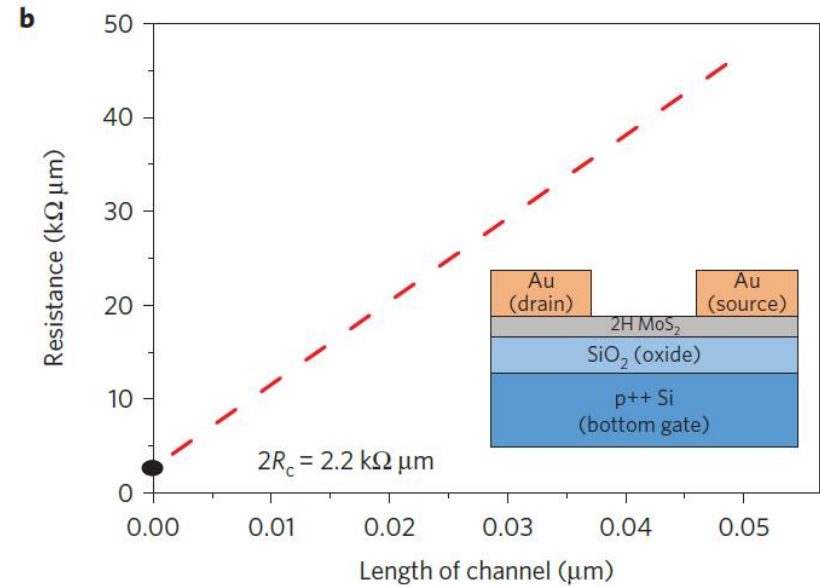
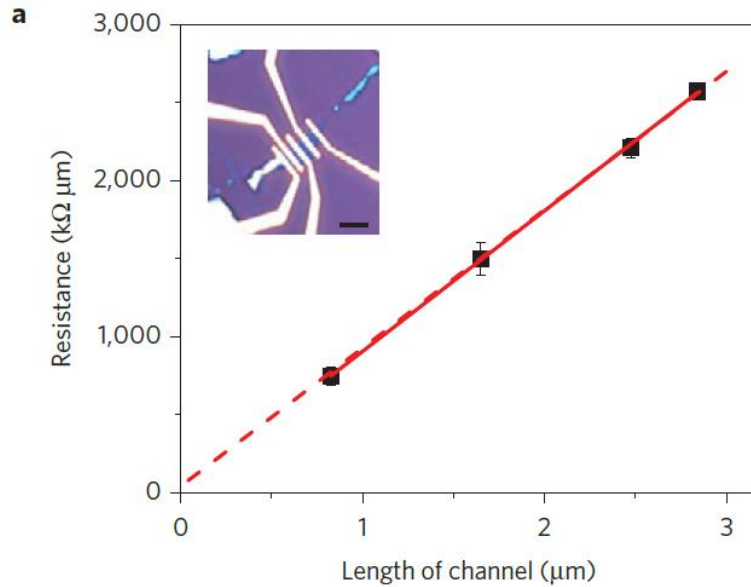
2H phase of MoS₂
semiconductor

1T phase
metallic



Phase engineering

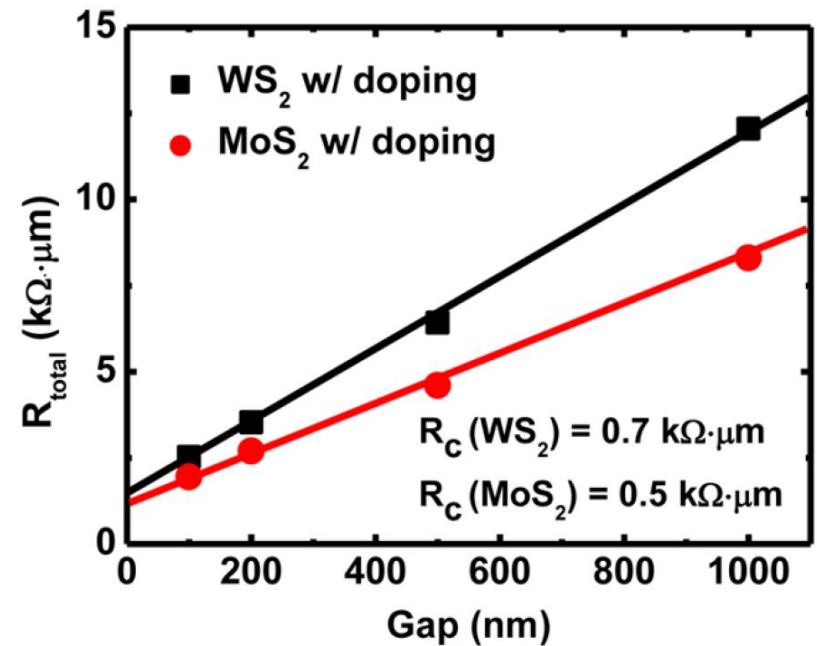
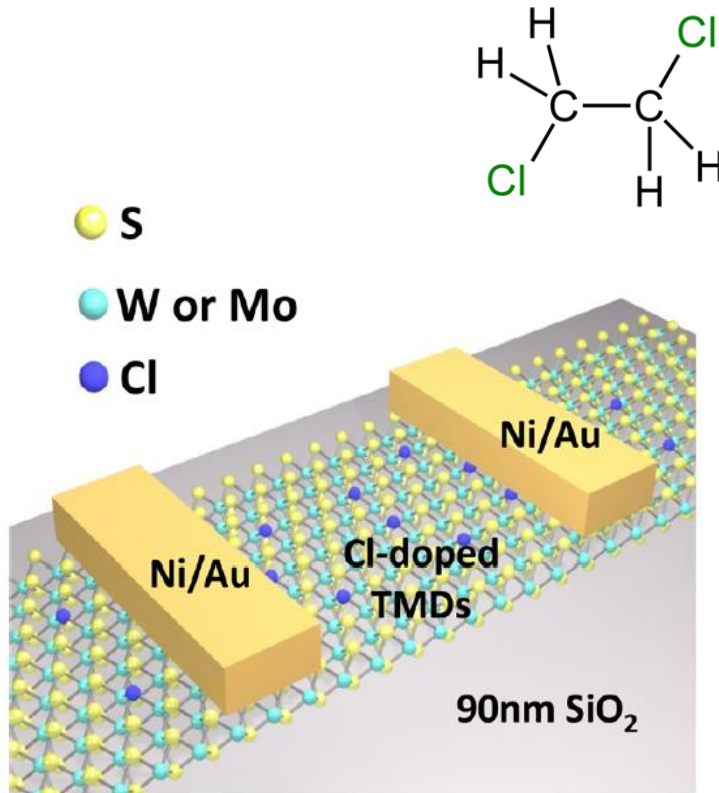
$$R_C = 200 - 300 \, \Omega \cdot \mu\text{m}$$



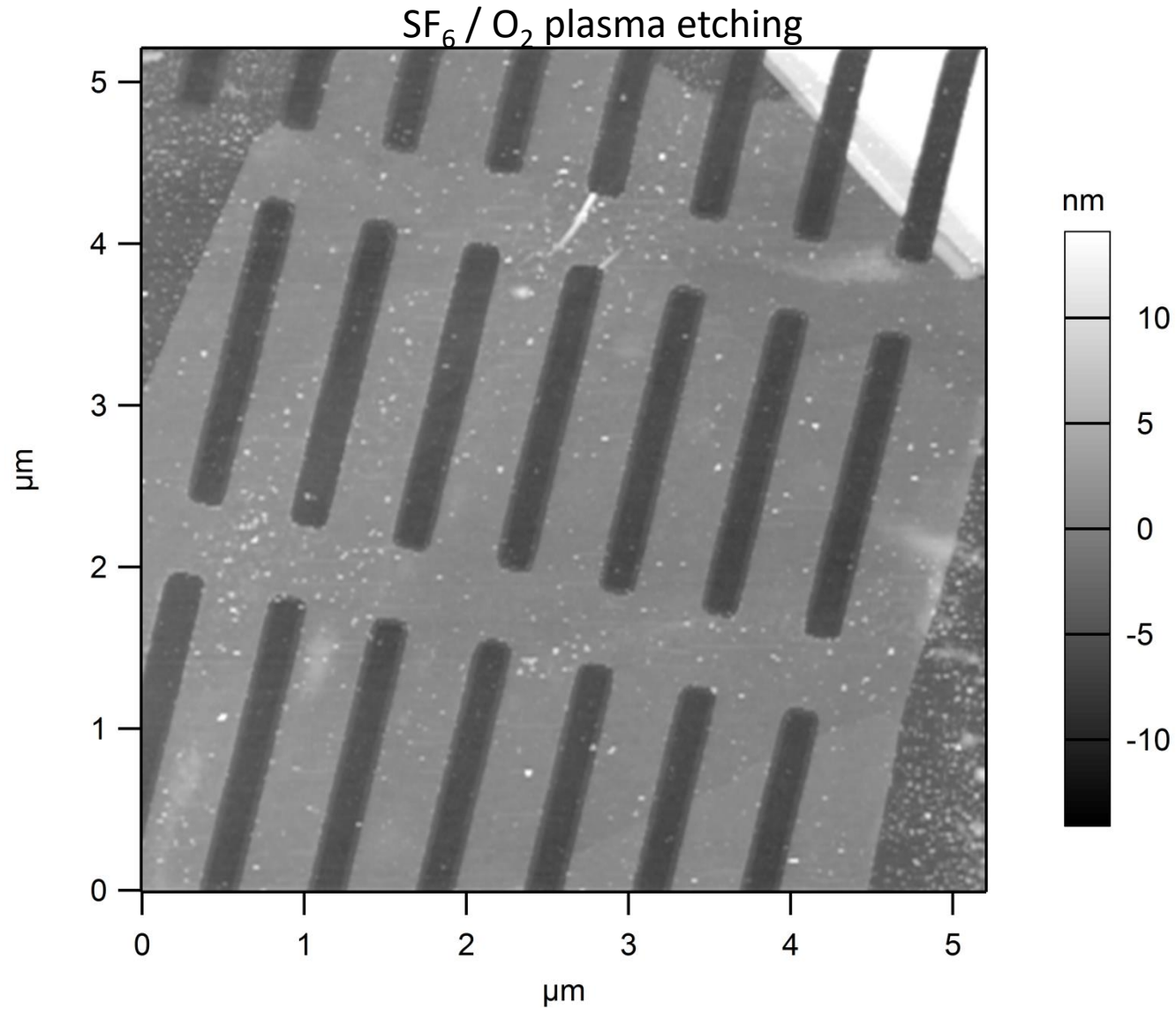
Doping

Cl doping by soaking the flakes in dichloroethane

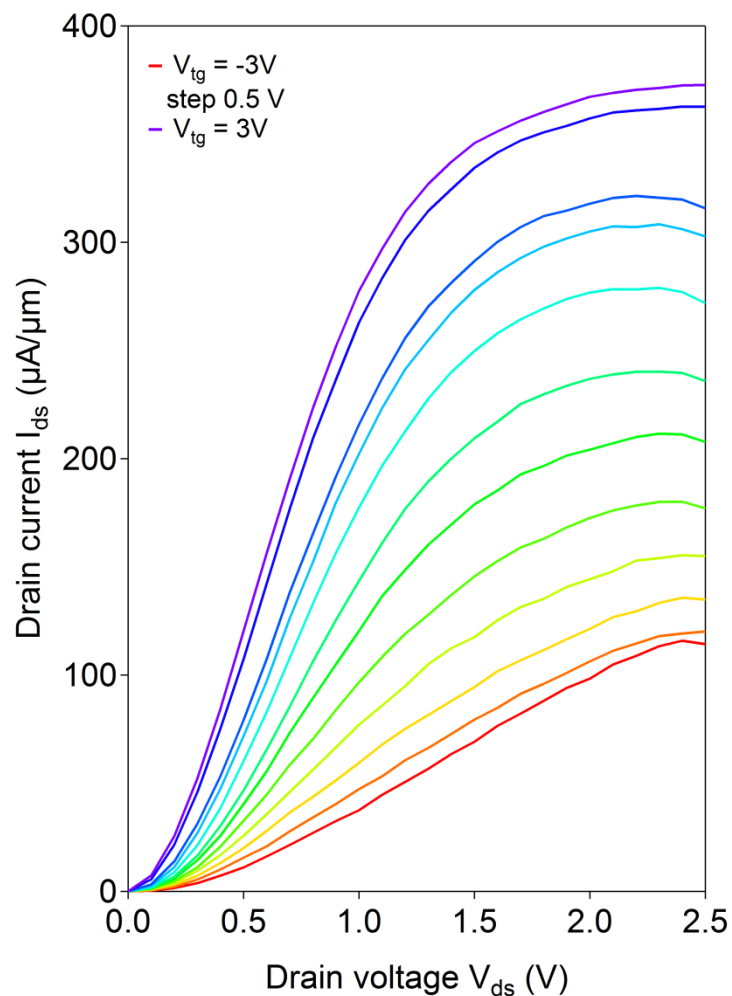
$$R_C \approx 500 \, \Omega \cdot \mu\text{m}$$



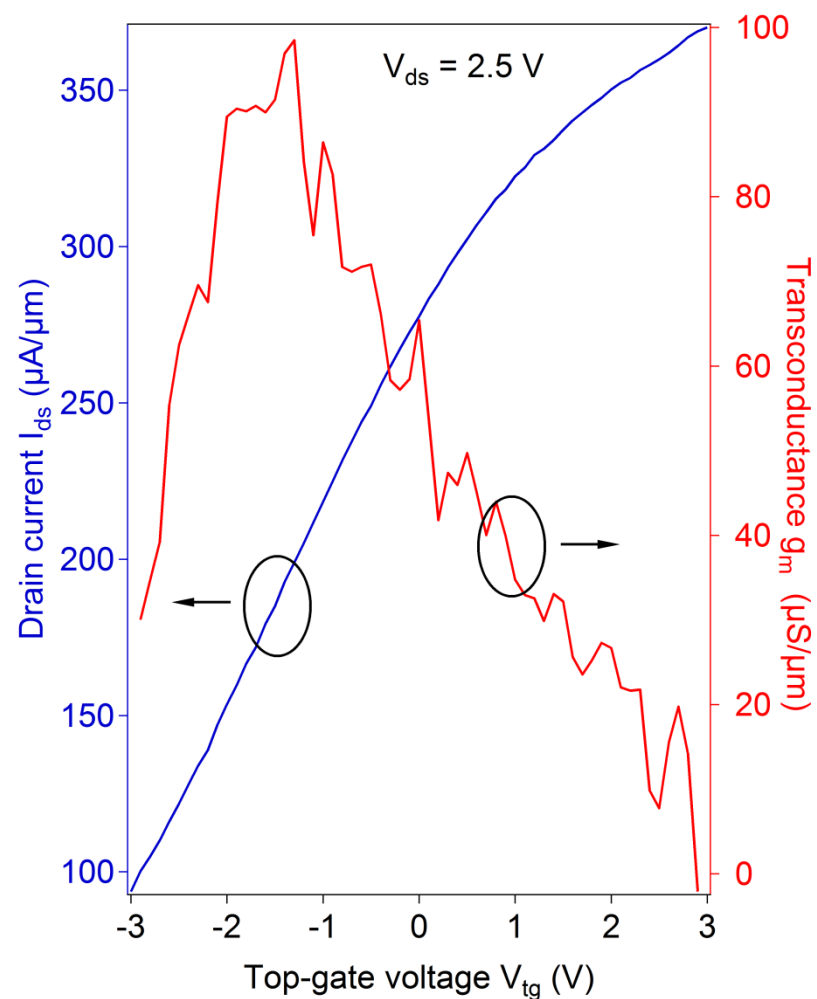
Edge contacts



Edge contacts



$$I_{\text{max}} = 370 \mu\text{A}/\mu\text{m}$$

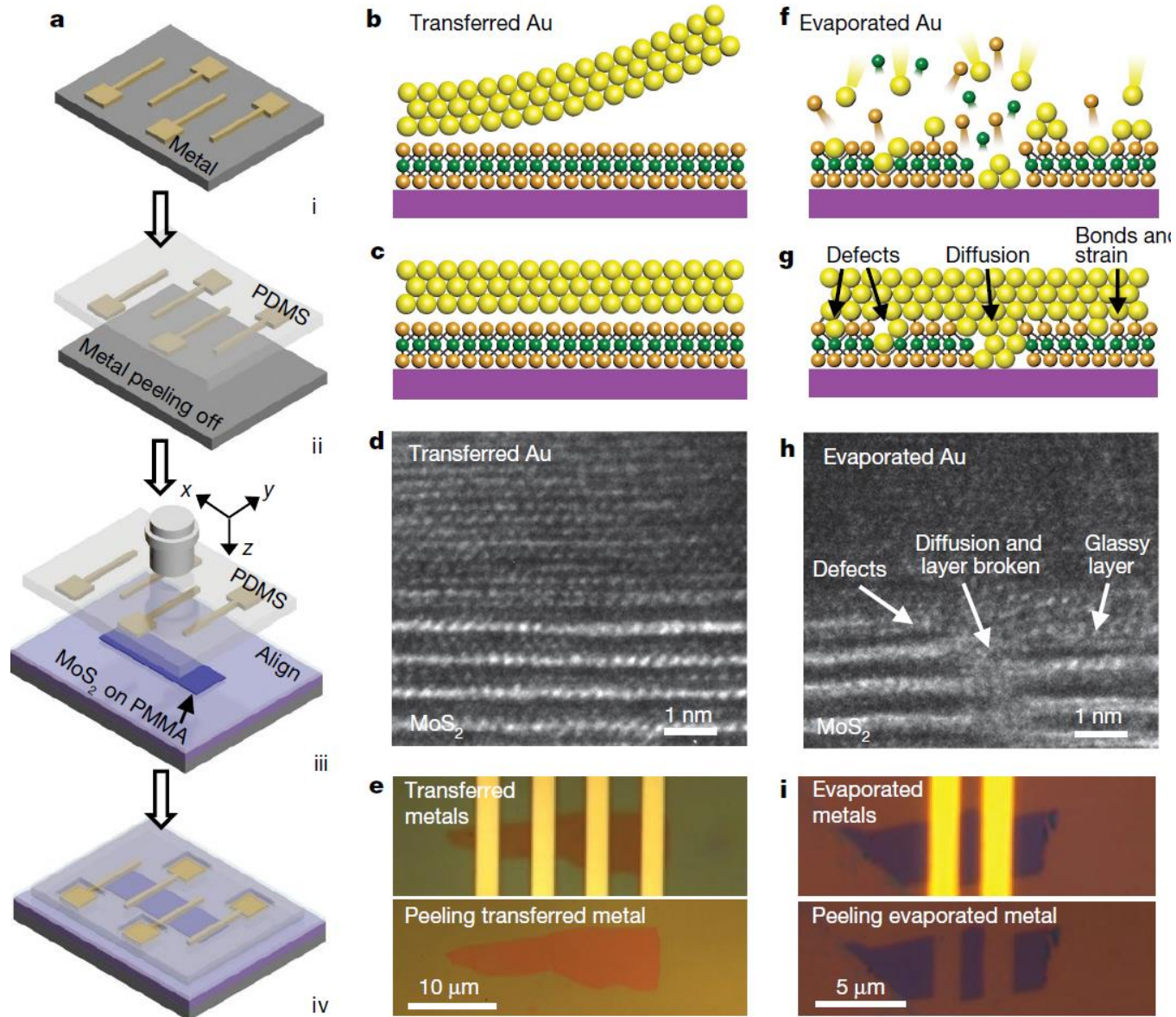


$$g_{m,\text{max}} = 98 \mu\text{S}/\mu\text{m}$$

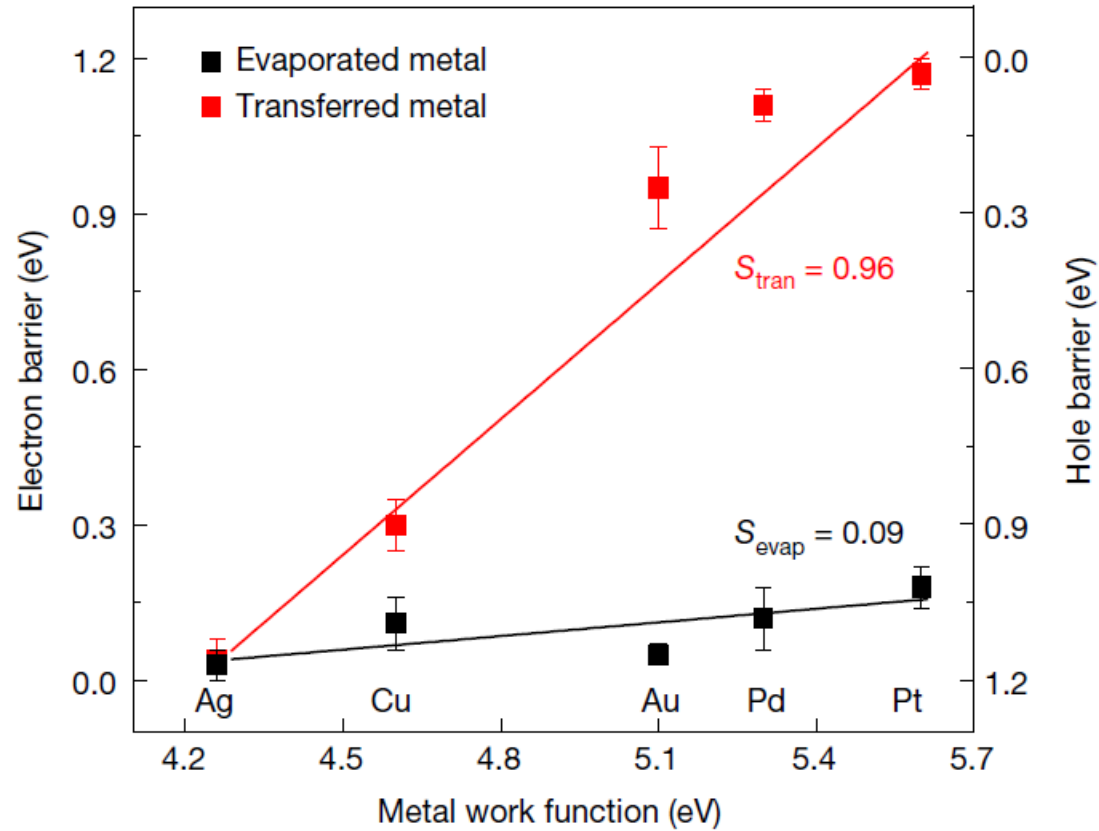
Pristine: $170 \mu\text{A}/\mu\text{m}$

$45 \mu\text{S}/\mu\text{m}$

Direct transfer of contacts onto 2D materials



Direct transfer of contacts onto 2D materials

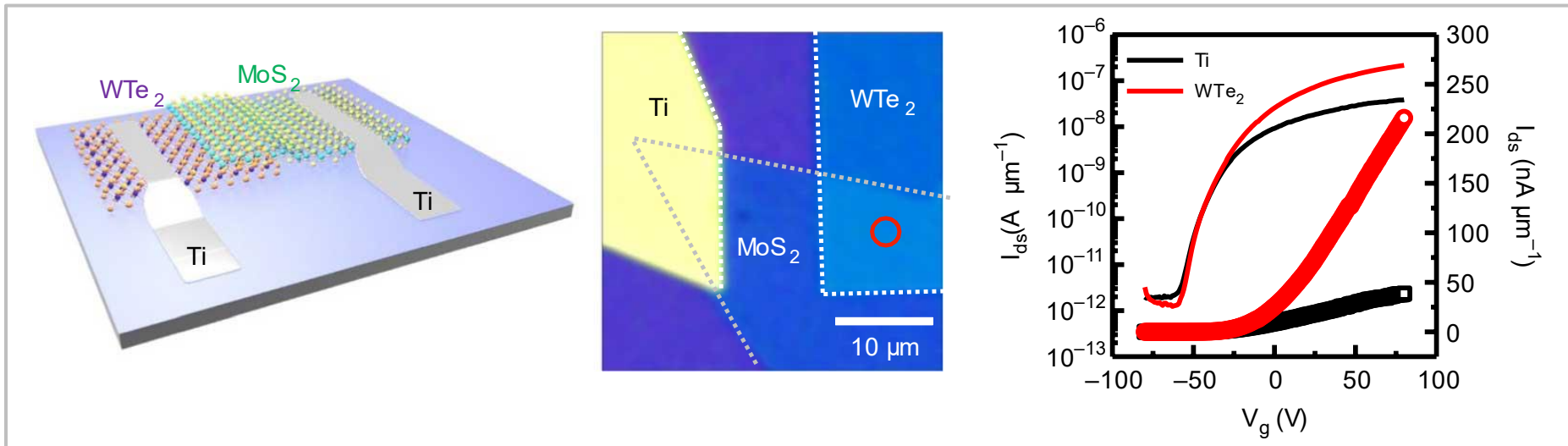
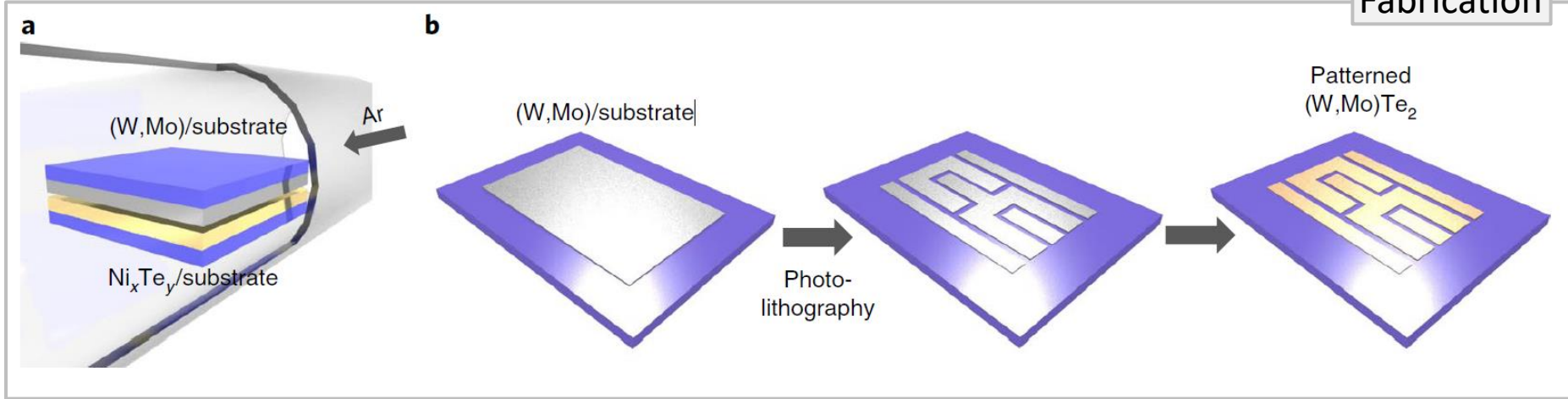


Liu et al. Nature (2018)

Direct transfer of 2D materials onto 2D contacts

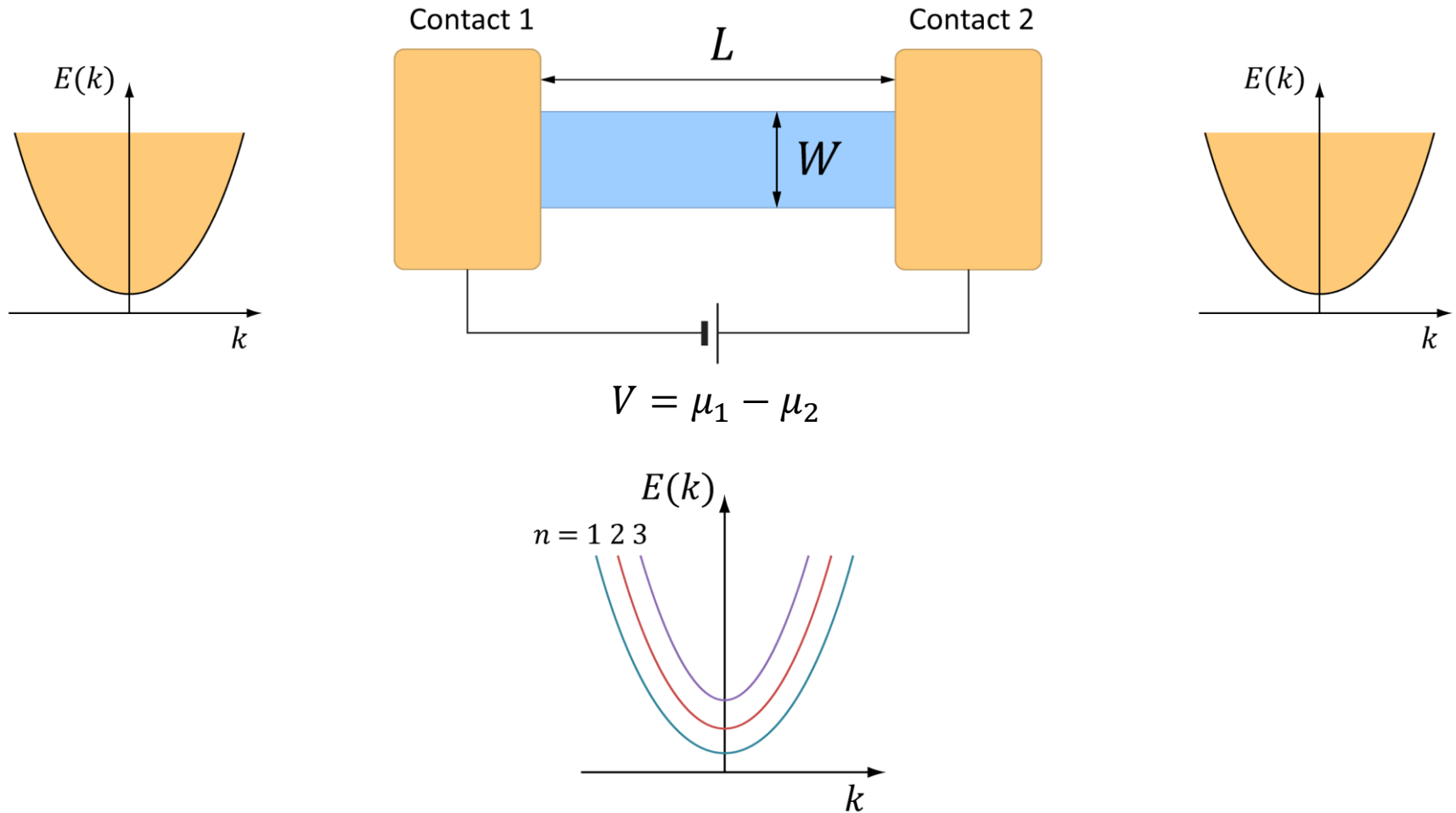
- MoTe₂ or WTe₂ contacts to MoS₂

Fabrication



Quantum resistance

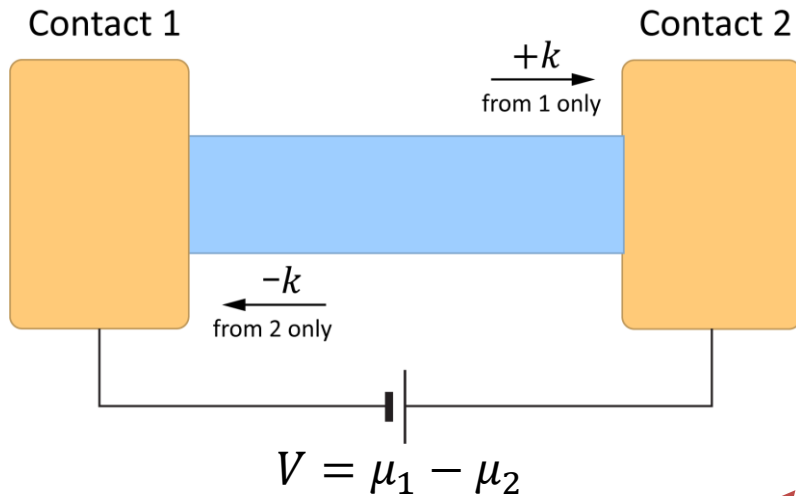
As the dimensions decrease, resistance approaches a limiting value R_C



Origin: conductor and contact pads are dissimilar materials (with and without confinement)

Quantum resistance for a ballistic conductor

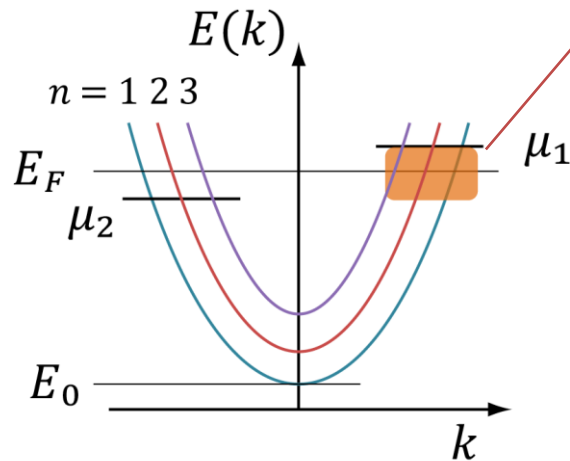
No scattering in the channel



$+k$ states: occupied only by electrons from contact 1

$-k$ states: occupied only by electrons from contact 2

Total current is carried by $+k$ states between μ_1 and μ_2



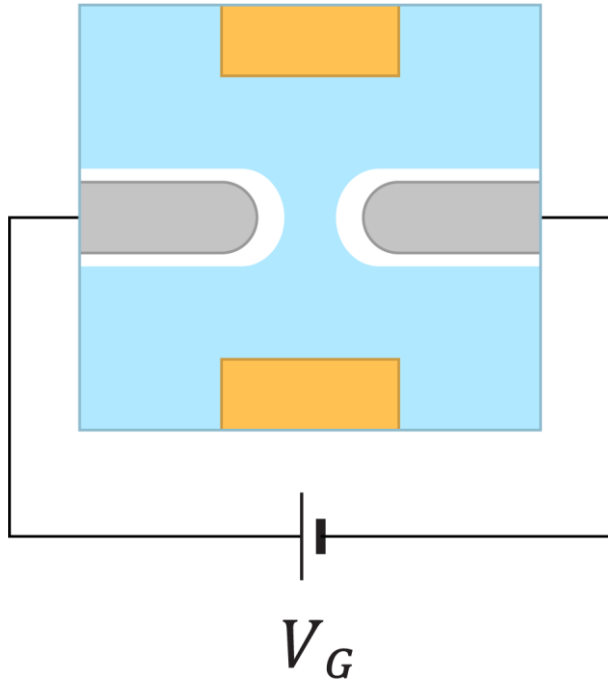
$$I = \frac{2e^2}{h} M \frac{\mu_1 - \mu_2}{e} = G_C V$$

$$G_C = \frac{2e^2}{h} M \quad \text{2 from spin degeneracy}$$

$$\frac{1}{G_C} = R_C = \frac{12.9 \text{ k}\Omega}{M}$$

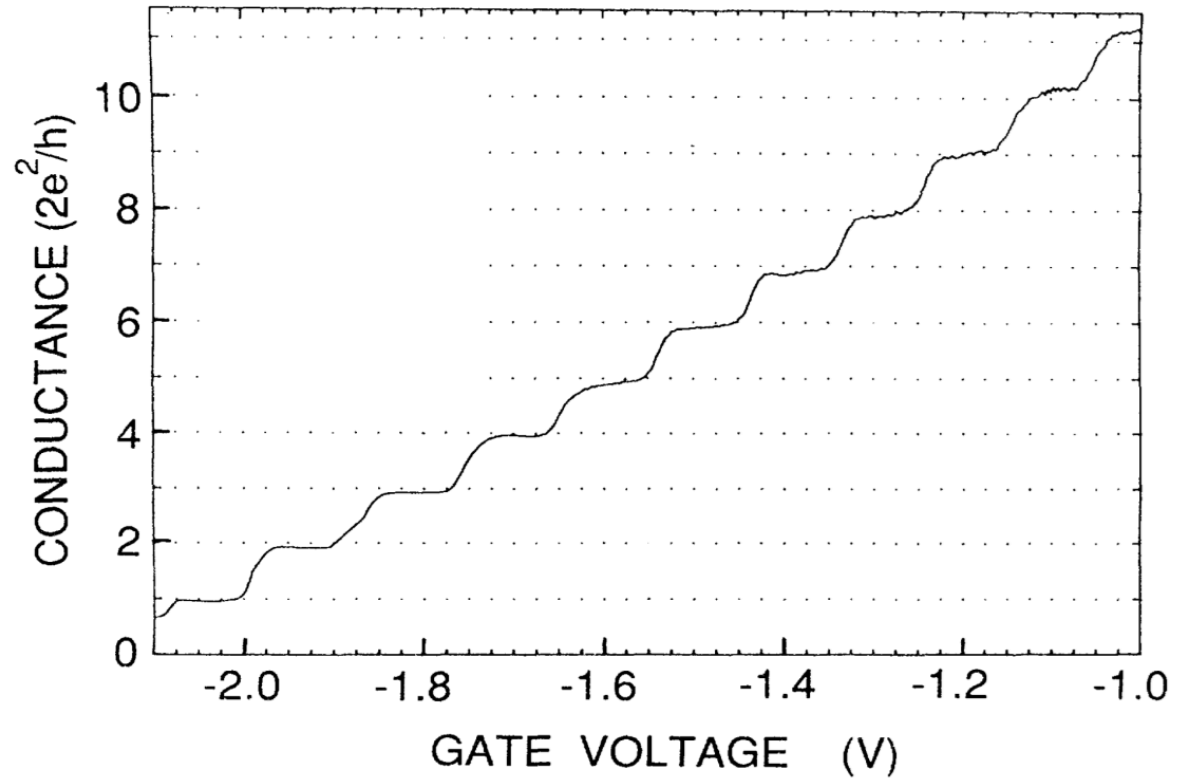
M number of modes (subbands)

Quantized conductance: GaAs



$$G_C = \frac{2e^2}{h} M$$

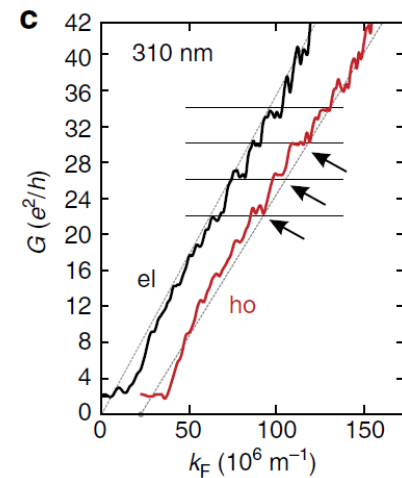
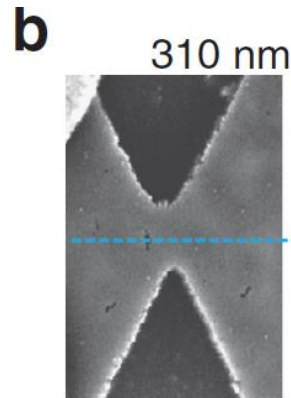
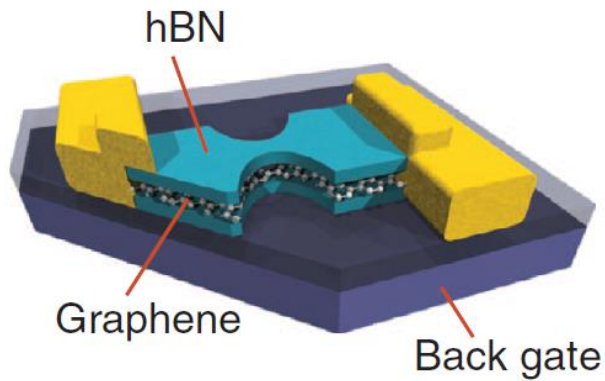
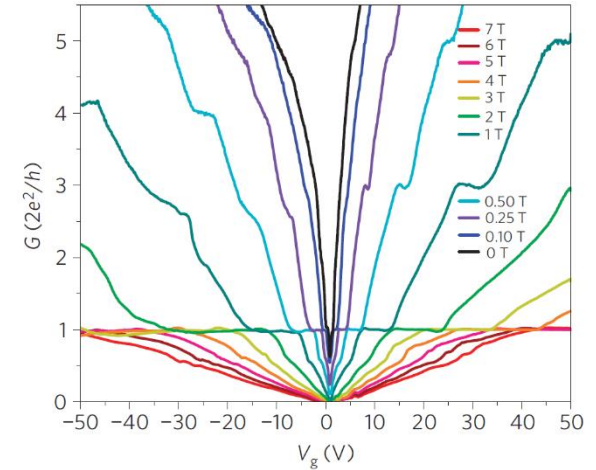
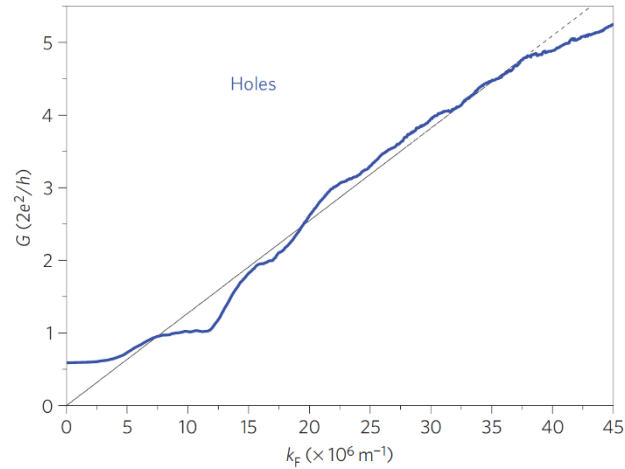
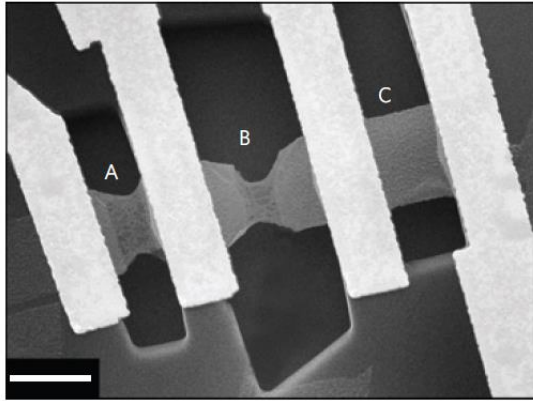
$$\lambda_F = 100 \text{ nm}$$



Van Wees et al., PRL 60, 848 (1988)

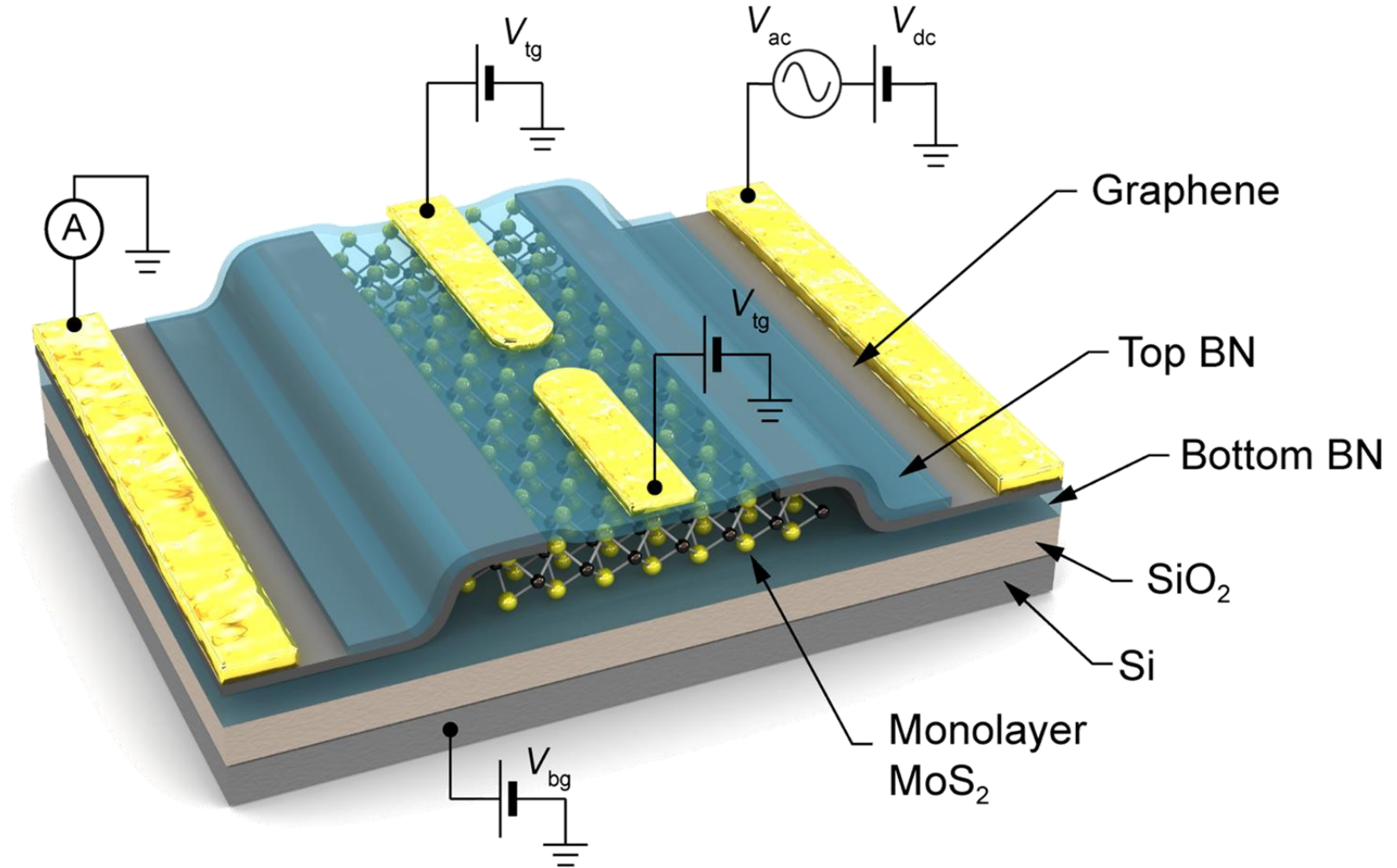
Van Wees et al., PRB 43, 12431 (1991)

Quantized conductance: graphene



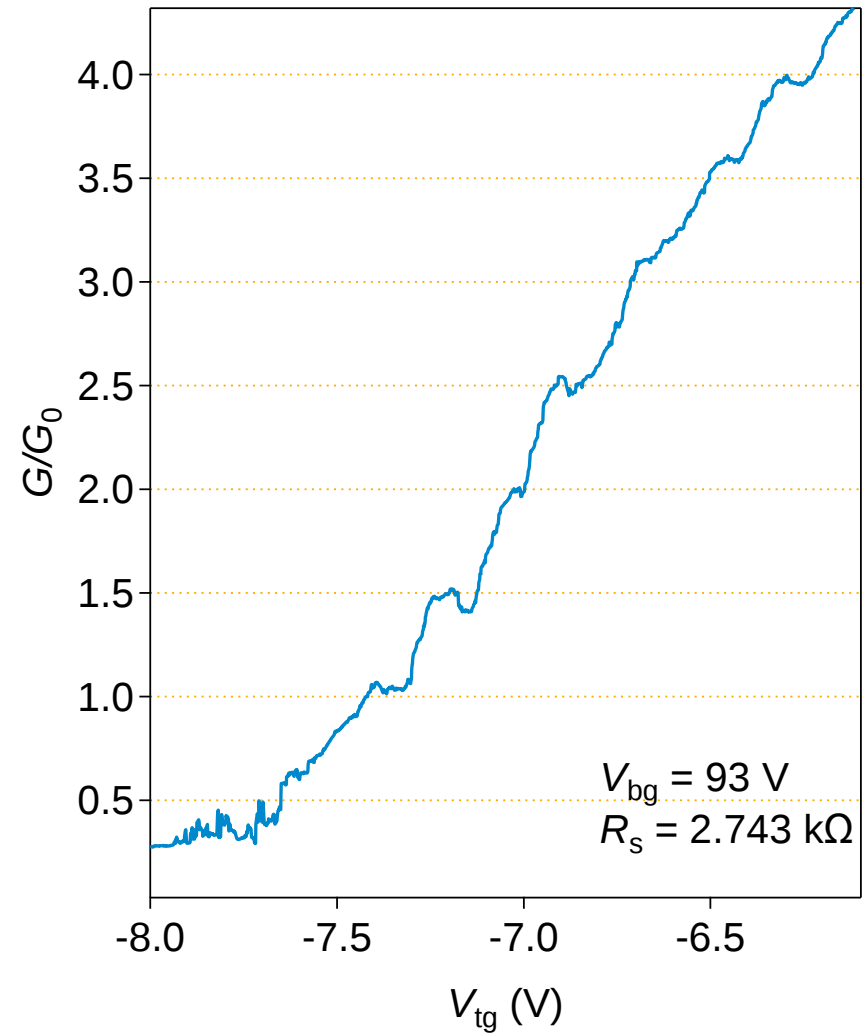
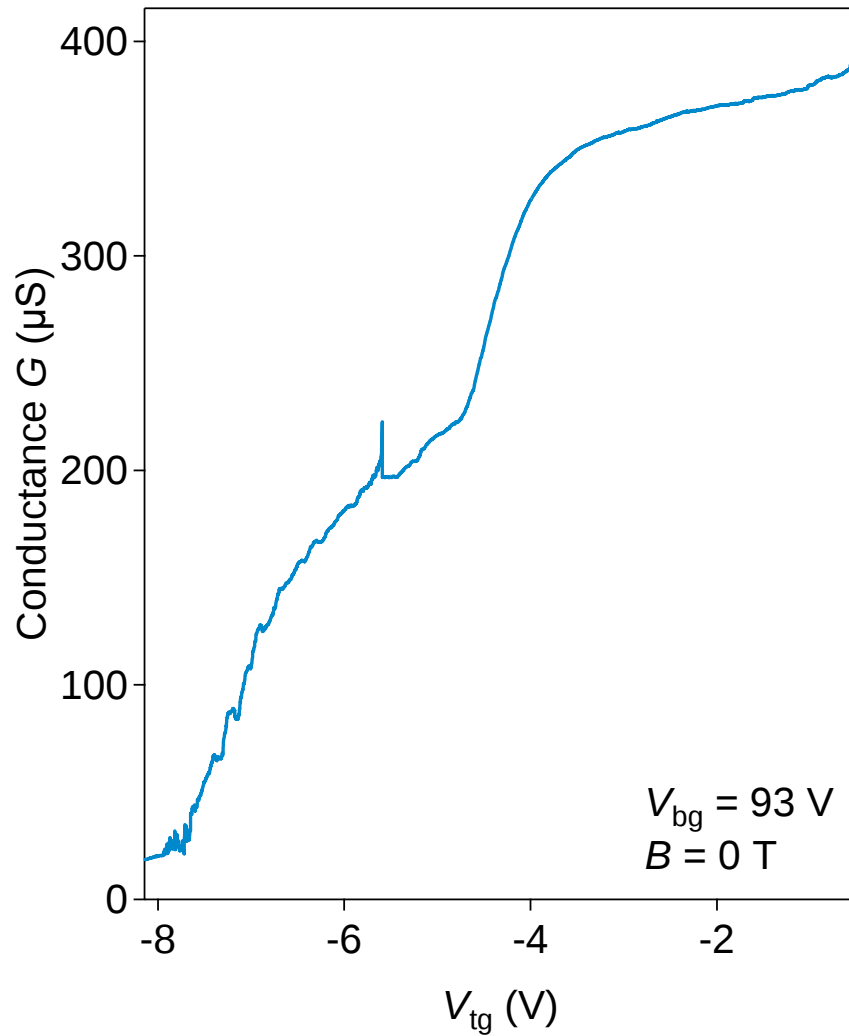
Tombros, Wees, et al. Nat. Phys. (2011)
Terrés, Stampfer, et al. Nat. Comm. (2016)

Quantized conductance: MoS₂



Marinov...Kis; Nature Comms. (2017)

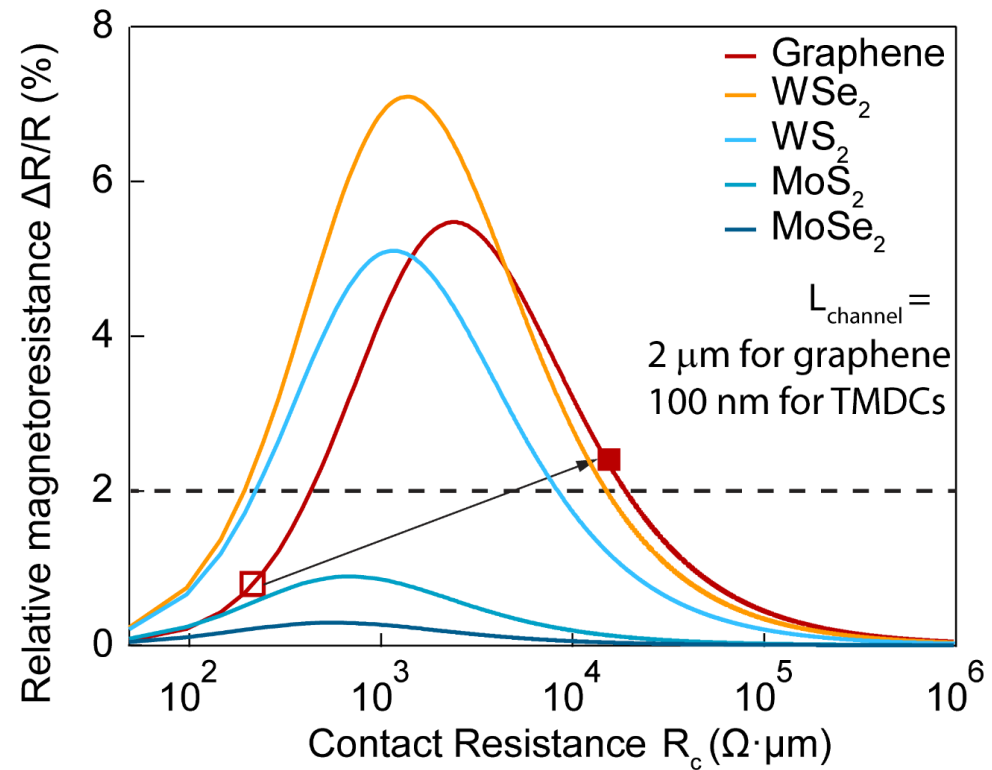
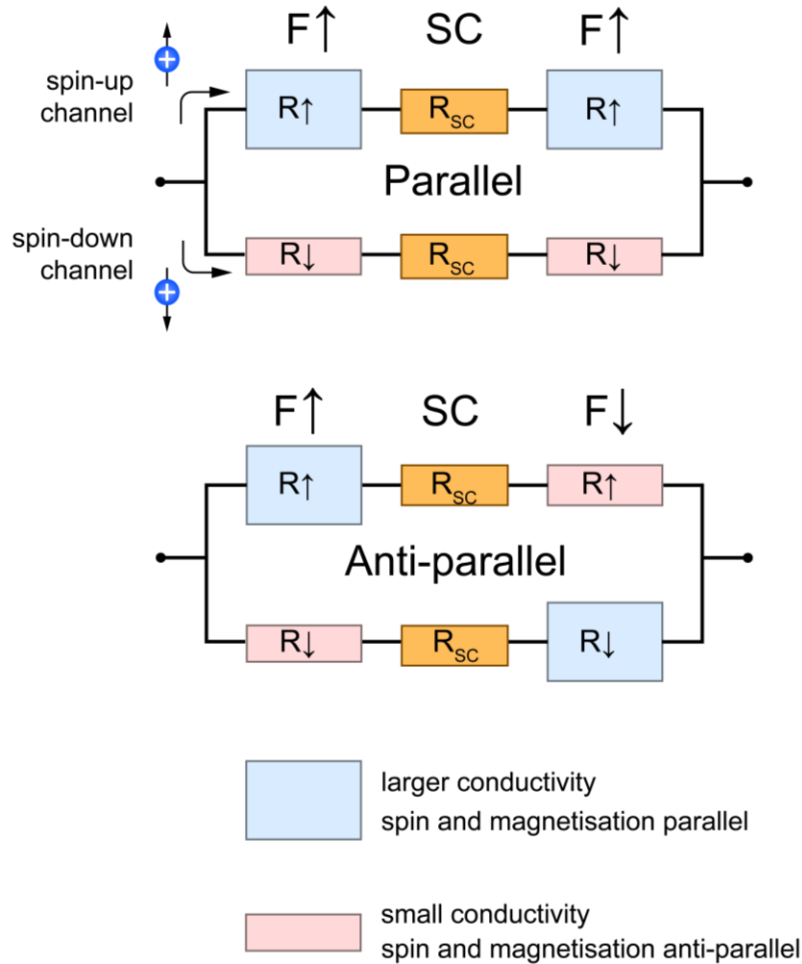
Quantized conductance: MoS₂



Steps of e^2/h : degeneracies lifted

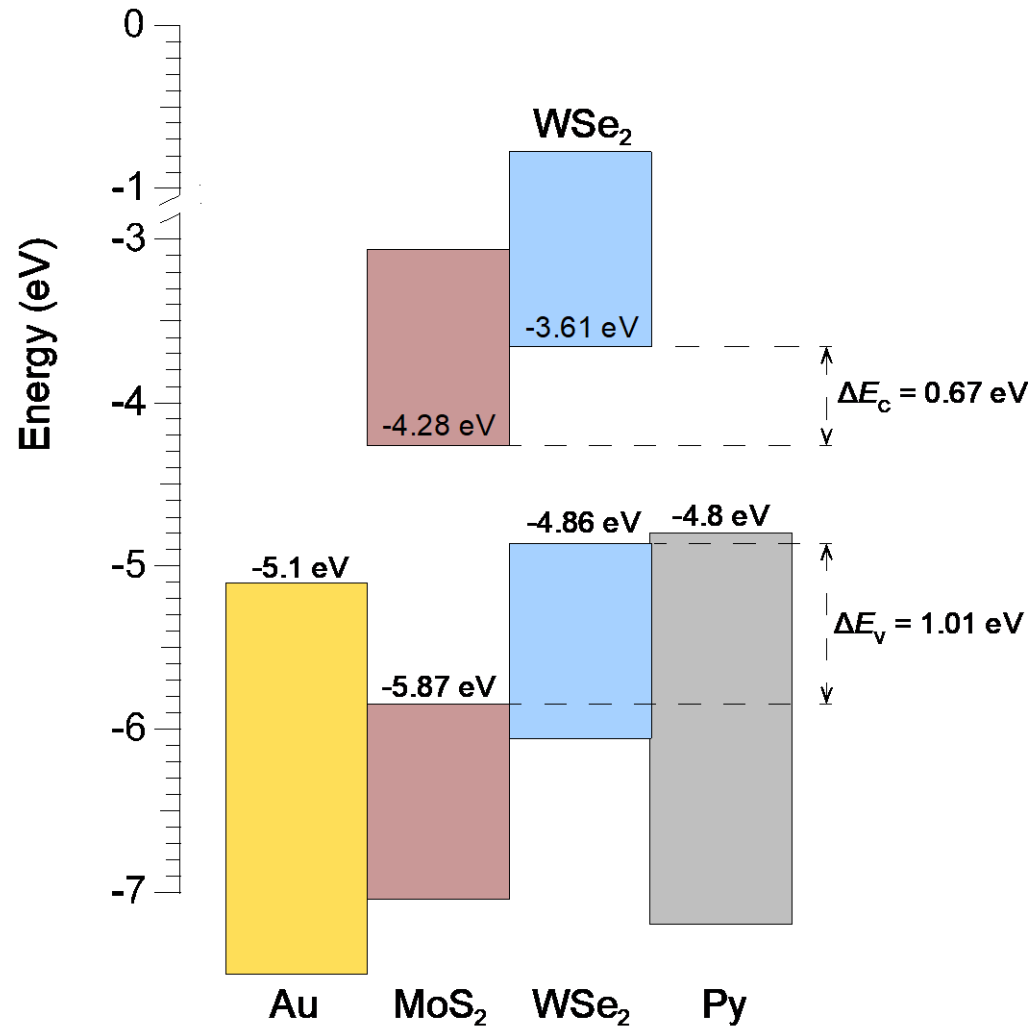
When low R_c is not good: spin injection

Conductivity mismatch problem



Allain...Kis; Nat. Materials (2015)

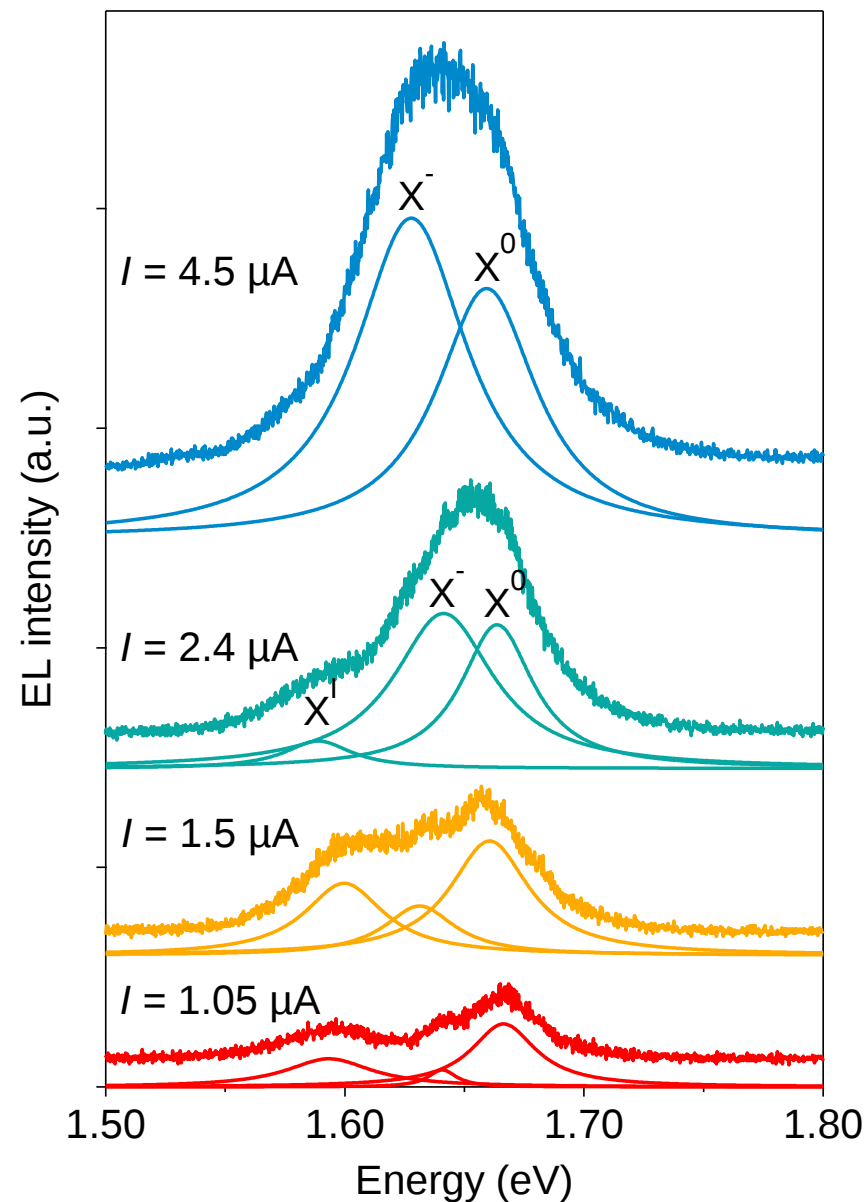
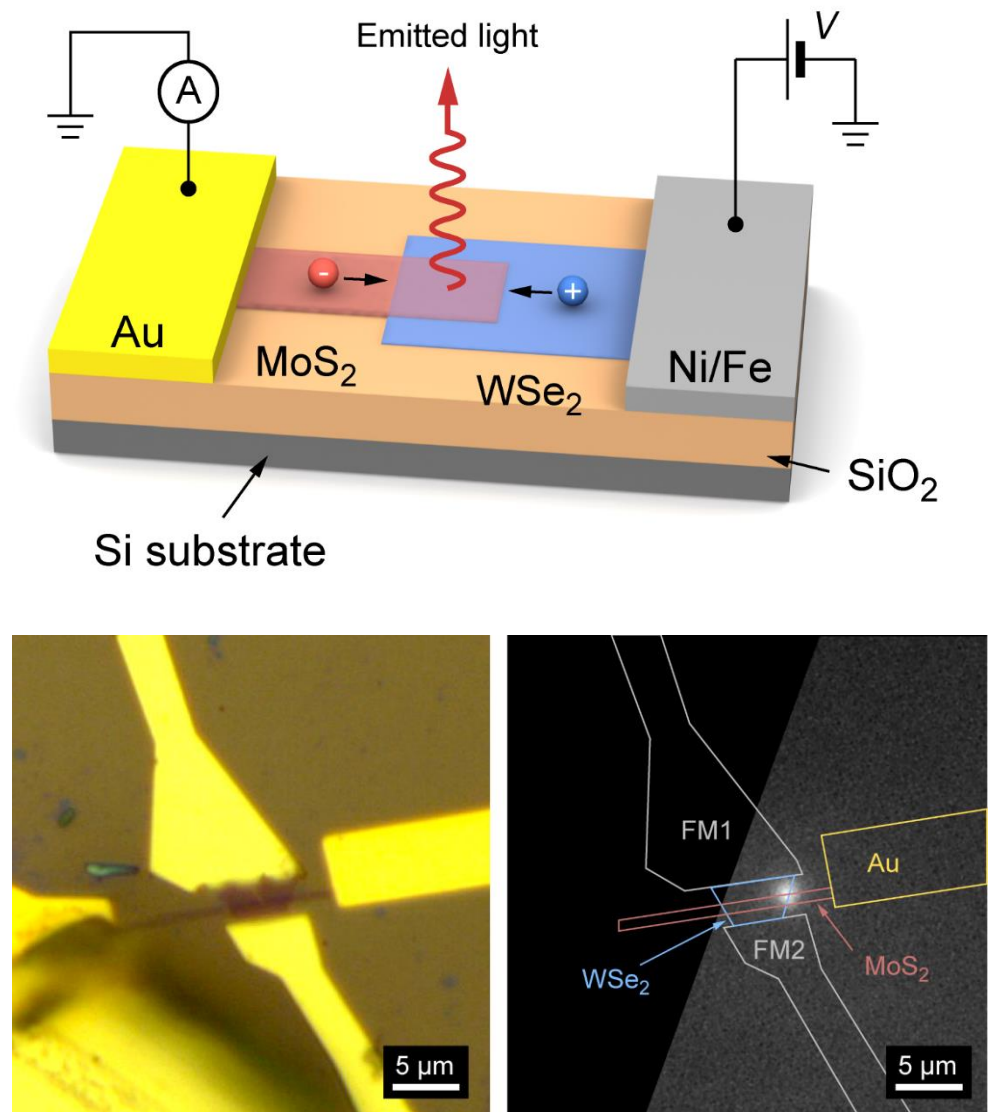
Permalloy Electrodes



Band alignment: Kang...Wu; Applied Physics Letters (2013)

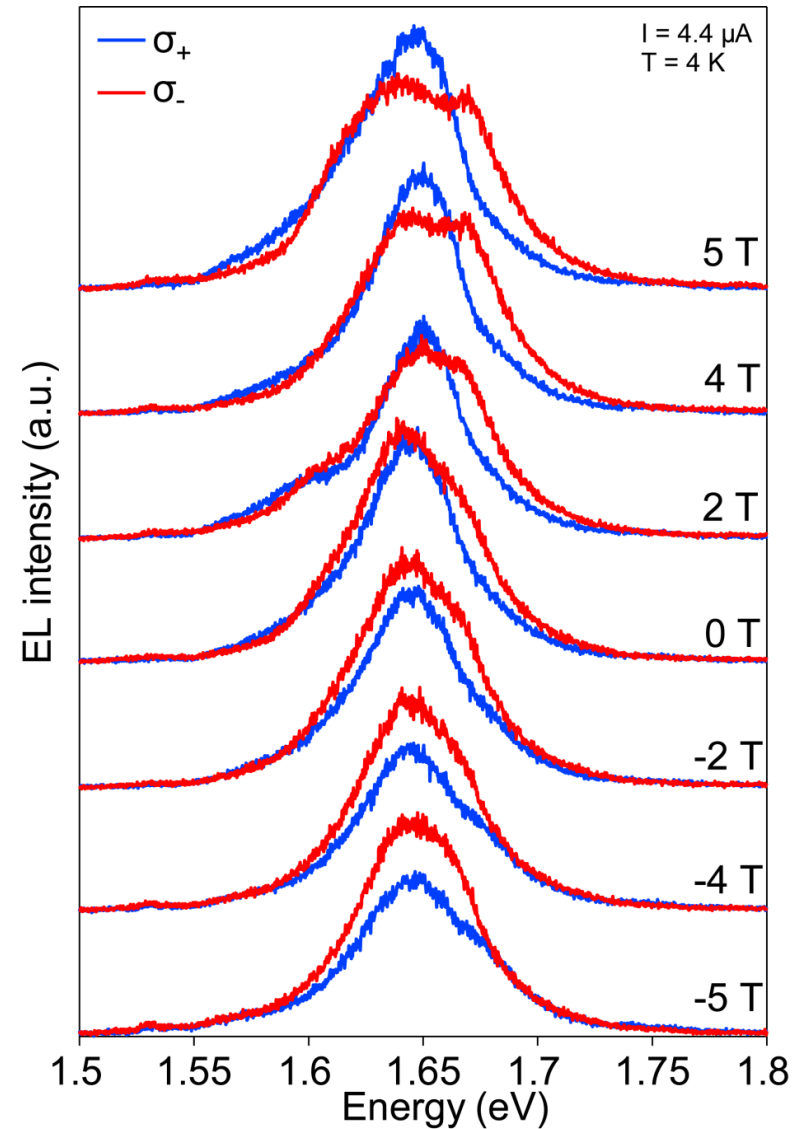
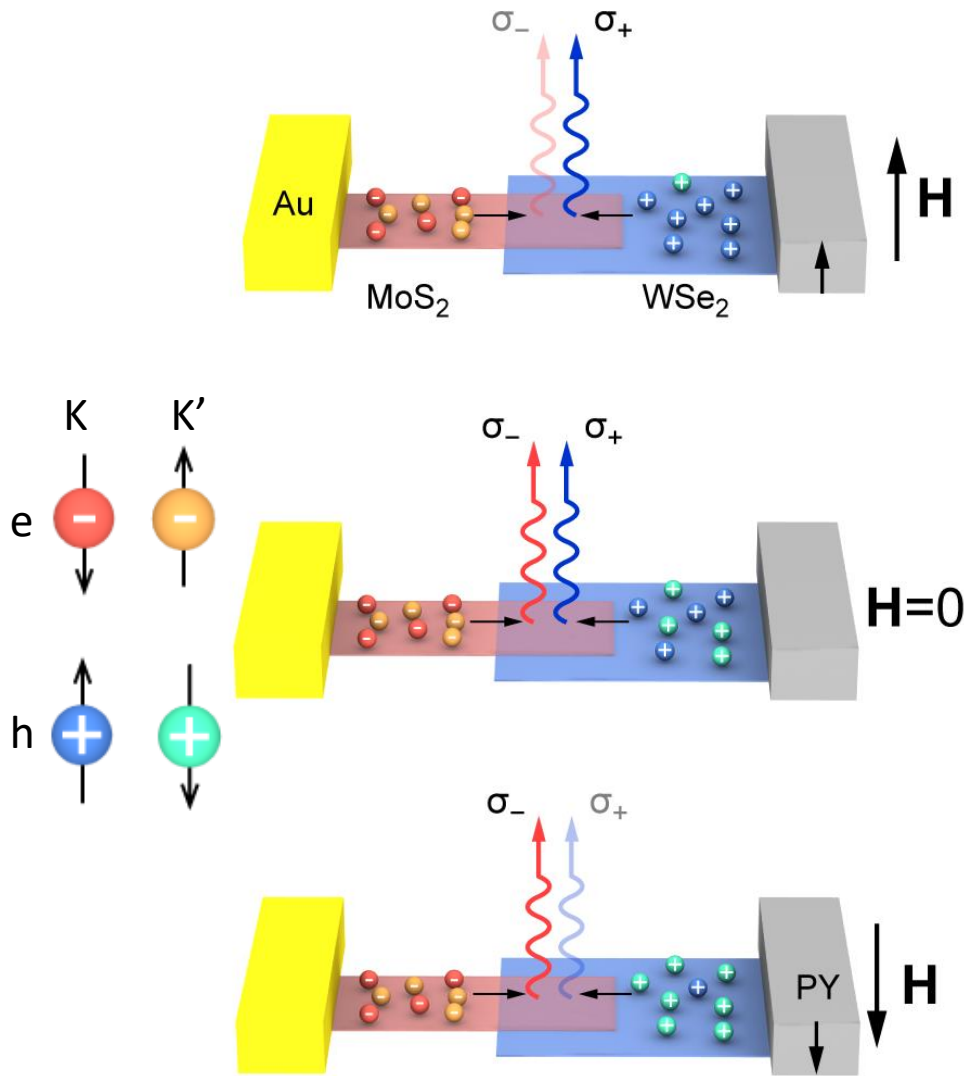
PY work function: Wang...Xiu; Sci. Rep. (2014)

Heterostructure LED with a Lateral FM Contact



Lopez Sanchez...Kis; Nano Lett. (2016)

Valley Polarization by Spin Injection



Lopez Sanchez...Kis; Nano Lett. (2016)

Recapitulation

Resistance scaling - general

- Devices limited by contact resistance
- Quantum limit of resistance
- Contact resistance can be measured using 4-probe and TLM

Contacts to 2D materials

- Contact geometries – edge, top and combination
- Contact resistance scaling – transmission line model
- Almost all current examples in the literature fall short of ITRS requirements
- Schottky barrier extraction from the flat band condition
- Fermi level pinning
- Strategies for reducing contact resistance: phase engineering, doping, etching contacts, transfer of contacts

Origins of the quantum limit

- Ballistic charge injection

Spin injection into 2D materials

- Conductivity mismatch problem

Thank you for your attention!